

LETTER

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To cite this article: K A M Hasan Siddiquee *et al* 2021 *J. Phys.: Condens. Matter* **33** 17LT01

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Letter

Fermi surfaces of the topological semimetal CaSn_3 probed through de Haas van Alphen oscillations

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Received 9 November 2020, revised 18 January 2021

Accepted for publication 28 January 2021

Published 20 April 2021



Abstract

In the search of topological superconductors, nailing down the Fermiology of the normal state is as crucial a prerequisite as unraveling the superconducting pairing symmetry. In particular, the number of time-reversal-invariant momenta (TRIM) in the Brillouin zone enclosed by Fermi surfaces is closely linked to the topological class of time-reversal-invariant systems, and can experimentally be investigated. We report here a detailed study of de Haas van Alphen quantum oscillations in single crystals of the topological semimetal CaSn_3 with torque magnetometry in high magnetic fields up to 35 T. In conjunction with density functional theory based calculations, the observed quantum oscillations frequencies indicate that the Fermi surfaces of CaSn_3 enclose an odd number of TRIM, satisfying one of the proposed criteria to realize topological superconductivity. Nonzero Berry phases extracted from the magnetic oscillations also support the nontrivial topological nature of CaSn_3 .

Keywords: quantum oscillations, topological superconductors, topological semimetals, de Haas van Alphen

(Some figures may appear in colour only in the online journal)

1. Introduction

Topological superconductors (TSCs) hosting Majorana fermions on the boundaries have recently attracted much attention because of potential application in quantum computing and other areas [1]. Although extensive studies to explore TSCs, such as metal-intercalated Bi_2Se_3 [1–4] and half Heusler systems [5, 6], have been conducted, unambiguous

experimental identification of topological superconductivity is still lacking.

According to a theory proposed by Fu and Berg [7], a time-reversal-invariant centrosymmetric superconductor is a topological superconductor, if it possesses the following properties: (1) odd-parity pairing symmetry with a full superconducting gap and (2) an odd number of time-reversal-invariant momenta (TRIM) in the Brillouin zone, enclosed by its Fermi surfaces. Together with the study of the superconducting gap structure in the superconducting state, detailed

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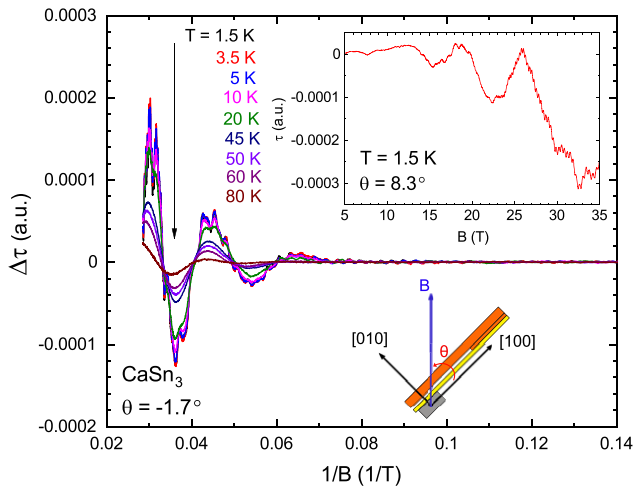


Figure 1. Temperature dependent oscillatory magnetic torque in CaSn_3 . Oscillatory part of magnetic torque as a function of $1/B$ at $\theta = -1.7^\circ$, where θ is the angle between the magnetic field and the $[100]$ axis while rotating the field from $[100]$ to $[010]$ in the (001) plane as illustrated in the lower inset. The oscillation amplitudes decrease with increasing temperatures. Upper inset: magnetic torque as a function of the magnetic field B for $\theta = 8.3^\circ$ at $T = 1.5$ K.

investigation of Fermiology in the normal state is crucial for identifying topological superconductivity in topological materials.

Recently, the binary stannide semimetal CaSn_3 has been proposed to be a promising candidate for realizing topological superconductivity, as it is predicted to be a topologically nontrivial semimetal [8]. The nontrivial electronic band structure harbors topological nodal lines in the absence of spin orbit coupling (SOC). Upon turning on SOC, the nodal lines evolve into topological point nodes [8]. More notably, superconductivity has experimentally been confirmed [9, 10], and the possible nontrivial Berry phase associated with the topological nature of CaSn_3 has been obtained from a recent quantum oscillation study in the normal state. However, it is still unclear that this system satisfies the proposed criterion for topological superconductors, i.e. an odd number of Fermi surfaces enclosing TRIM in the Brillouin zone.

Here we present a detailed study of de Haas van Alphen (dHvA) oscillations in CaSn_3 with torque magnetometry in high magnetic fields up to 35 T. dHvA measurements provide comprehensive information about Fermi surfaces, as does angle-resolved photoemission spectroscopy, which has been used successfully to reveal band structures of topological materials [11]. In addition, from dHvA oscillations we can extract topological properties of materials. In CaSn_3 , we observe four fundamental dHvA frequencies associated with the Fermi surfaces as well as strong Zeeman splitting. With the aid of our band structure calculations, we assign the measured frequencies to the Fermi surfaces of CaSn_3 , unveiling that an odd number of TRIM is enclosed by the Fermi surfaces. Combined with the observation of nontrivial Berry phases, this finding suggests that CaSn_3 is a promising material to realize topological superconductivity.

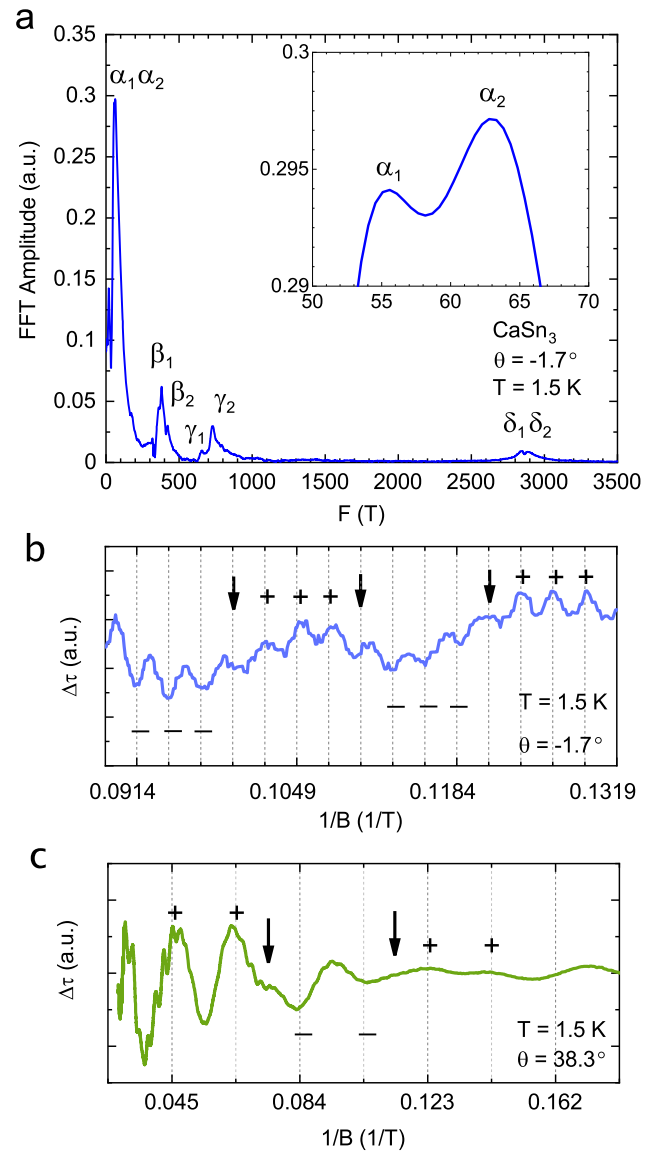


Figure 2. FFT spectrum of oscillatory magnetic torque and peak splitting in CaSn_3 . (a) FFT spectrum of oscillatory magnetic torque for $\theta = -1.7^\circ$ at $T = 1.5$ K (field range 5–35 T). Four fundamental frequencies, F_α , F_β , F_γ , and F_δ , with splittings are observed. Inset: peak splitting in the α orbit at $T = 1.5$ K. We observe beating due to two oscillatory components associated with (b) the β orbit with the periodicity of 0.0027 T^{-1} ($F \sim 370$ T) for $\theta = -1.7^\circ$ at $T = 1.5$ K, and (c) the α orbit with the periodicity of 0.0195 T^{-1} ($F \sim 50$ T) for $\theta = 38.3^\circ$ at $T = 1.5$ K. Arrows indicate nodes in the beating patterns. Plus and minus signs indicate the positions of the maxima and minima of the oscillations, respectively.

2. Methods

Single crystals of CaSn_3 were grown by a Sn self flux method. The starting elements with a ratio of $\text{Ca}:\text{Sn} = 1:9$ were placed in an alumina crucible, which in turn was sealed in a quartz tube. The mixture was heated up to 800°C , kept for 24 h, and cooled slowly down to 300°C at a rate of 2°C h^{-1} . The excess of Sn flux was decanted by centrifugation. We confirmed the cubic AuCu_3 -type structure with space group $Pm\bar{3}m$ with the lattice constant of $a = 4.7331(5) \text{ \AA}$ via

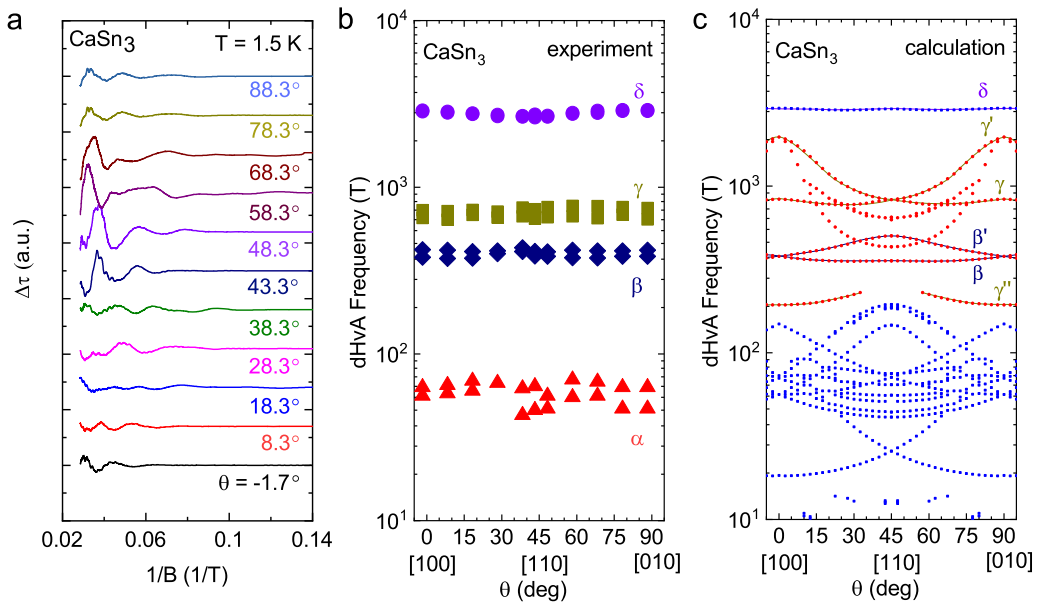


Figure 3. Angular dependence of dHvA oscillation frequencies. (a) Angular dependence of the oscillatory part of magnetic torque as a function of $1/B$. Reflecting the cubic crystal structure, the oscillations are symmetric with respect to $\theta \sim 45^\circ$. (b) Angular dependence of dHvA oscillation frequencies. The observed frequencies F_α , F_β , F_γ , and F_δ are nearly independent of angle θ . (c) Theoretical results obtained from DFT calculations using the SKEAF code for band 25 (blue) and band 26 (red).

powder x-ray diffraction. No Sn impurities were observed unlike the previous reports [9, 10]. Torque magnetometry was performed using a capacitive cantilever in a 35 T resistive magnet at the National high magnetic field laboratory, Tallahassee, FL.

The band structure and Fermi surfaces are calculated by means of density functional theory (DFT) employing the projector-augmented wave pseudopotential method [12, 13] and a plane-wave basis set as implemented in the Vienna *ab initio* simulation package [14, 15]. Exchange correlation effects are included via the generalized-gradient approximation in the form of Perdew–Berke–Enzerhoff (PBE) exchange–correlation functionals [16, 17]. We set a cutoff energy of 500 eV for plane-wave expansion, and adopt the DFT + U approach [18] to mitigate the lack of electron correlation in the PBE functionals. The effective Hubbard U parameter is chosen to be 2.55 eV to produce a lattice parameter 4.741 Å, close to a value of 4.742 Å that was determined experimentally [9] and not far from our measured value, $a = 4.7331(5)$ Å. All electronic iterations converged with 0.01 meV threshold. We use a Gaussian smearing of 0.1 eV and sample the Brillouin Zone with a $15 \times 15 \times 15$ Γ -centered grid. SOC is incorporated in the calculations of electronic band structure of the system. We calculate eigenvalues for all k -points of a $41 \times 41 \times 41$ uniform grid.

3. Results and discussion

3.1. Quantum oscillations in CaSn_3

Our torque magnetometry data exhibit clear dHvA oscillations. Upon applying magnetic field at $\theta = 8.3^\circ$, where θ is

the angle between the applied magnetic field and the [100] axis in the (001) plane, the oscillations in the magnetic torque τ are discernible above ~ 5 T at 1.5 K (figure 1 inset). The magnitudes of the oscillatory part of the magnetic torque $\Delta\tau$ decrease rapidly with increasing temperature (figure 1). While the fast oscillations are completely suppressed above 20 K, the slow oscillations can be observed up to at least 80 K.

Fast Fourier transform (FFT) allows us to determine the frequencies of oscillation components measured at $\theta = -1.7^\circ$ [figure 2(a)]. We find four fundamental frequencies F_α , F_β , F_γ , and F_δ . Each of them in fact consists of two frequencies close to each other [figure 2(a) and the inset], identified to be $F_{\alpha 1} = 56$ T, $F_{\alpha 2} = 63$ T, $F_{\beta 1} = 380$ T, $F_{\beta 2} = 422$ T, $F_{\gamma 1} = 655$ T, $F_{\gamma 2} = 729$ T, $F_{\delta 1} = 2845$ T, and $F_{\delta 2} = 2890$ T. This pairing of close frequencies is corroborated by clear beating patterns in the magnetic torque as a function of $1/B$. As indicated by arrows in figures 2(b) and (c), nodes in the beating patterns produce π phase shifts in the oscillations. While the frequencies of F_α , F_β , and F_γ are in good agreement with those previously reported [10], F_δ that is prominent above 30 T (or $1/B < 0.033$ T $^{-1}$) is newly identified by the present work.

The observed frequencies F are associated with extremal cross sectional areas, S , of the Fermi surfaces in the momentum space by the Onsager relation $F = (\hbar/2\pi e)S$. Tracking the extremal cross sectional areas in rotating magnetic fields about the crystallographic axes, we can trace the Fermi surface topology of CaSn_3 . The angular dependence of dHvA oscillations in CaSn_3 about the [001] axis is plotted in figure 3(a). As expected for the cubic structure of CaSn_3 , we observe symmetric behavior in the magnetic torque with respect to $\theta \sim 45^\circ$, similar to the previous report [10]. The dHvA

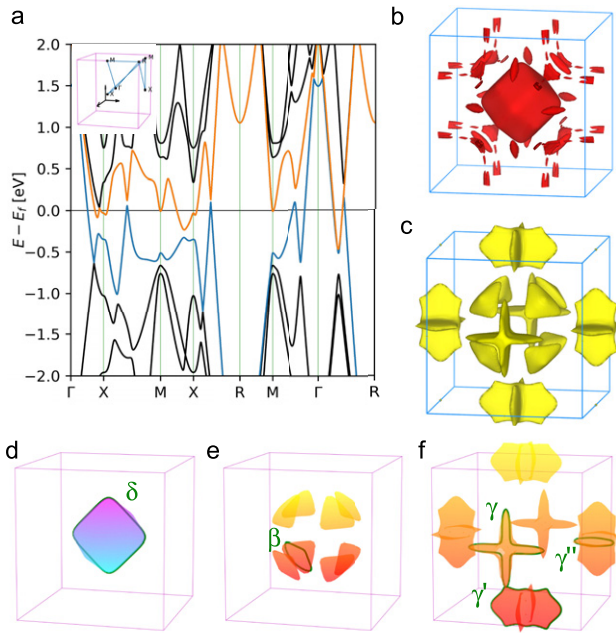


Figure 4. Electronic band structure and Fermi surfaces of CaSn_3 . (a) Band structure of CaSn_3 calculated by DFT. The local minimum of the electron band (shown in orange) at the M point is very close to the Fermi energy E_F , suggesting that the sizes of Fermi pockets at the M points are extremely sensitive to E_F . Inset: high symmetry points in the Brillouin zone. (b) Fermi surfaces of band 25 (hole). A large hole pocket is located around the Γ point, surrounded by numerous tiny hole pockets. (c) Fermi surfaces of band 26 (electron), consisting of cross-shaped electron pockets around the X points, triangle-shaped electron pockets between the Γ and R points, and small electron pockets around the M points. Calculated dHvA orbits for (d) δ , (e) β , (f) γ , γ' , and γ'' . Corresponding frequencies are plotted in figure 3(c).

frequencies extracted from the FFT analysis exhibit nearly isotropic angular dependence for the α , β , γ , and δ orbits, as shown in figure 3(b).

3.2. Fermi surfaces of CaSn_3

To compare with the experimental observations, we show the calculated band structure of CaSn_3 in figure 4(a). The predicted bands consist of a hole band (band 25) and an electron band (band 26). Band 25 comprises a large hole pocket around the Γ point in the Brillouin zone, surrounded by numerous small hole pockets [figure 4(b)], and band 26 has cross-shaped electron pockets around the X points and triangle-shaped electron pockets located between the Γ and R points, along with tiny electron pockets around the M points [figure 4(c)]. The calculated band structure agrees with the one previously reported in reference [8]. Figure 3(c) shows theoretical quantum oscillation frequencies generated from the DFT calculations using the supercell K-space extremal area finder (SKEAF) code [19].

On comparing the theoretical oscillation frequencies with the observed ones, we can allocate the frequencies to corresponding Fermi surfaces of CaSn_3 . The δ orbit with $F_\delta \sim 2900$ T corresponds well to the large hole pocket around the Γ point [figure 4(d)]. The β orbit with $F_\beta \sim 400$ T is close to the frequency branch of triangle-shaped electron pockets

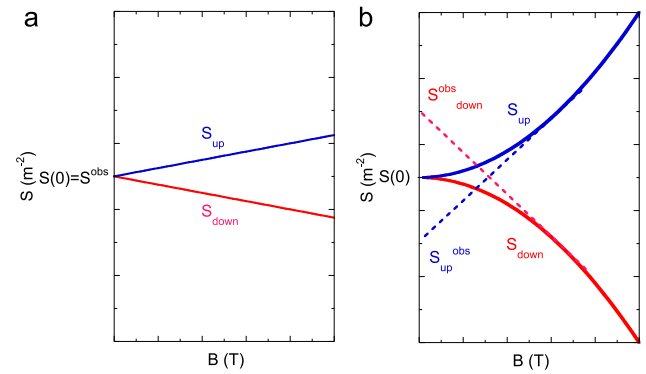


Figure 5. Spin-splitting of Fermi surface due to nonlinear Zeeman effect. (a) Magnetic field dependence of the extremal cross-sectional areas for spin-up and down Fermi surfaces S_{up} and S_{down} due to the linear Zeeman effect. The observed extremal cross-sectional area $S^{\text{obs}} = S(B) - BdS(B)/dB$ is identical to the zero-field limit of cross-sectional area $S(0)$, leading to $S_{\text{up}}^{\text{obs}} = S_{\text{down}}^{\text{obs}}$. (b) Magnetic field dependence of the extremal cross-sectional areas for spin-up and spin-down Fermi surfaces due to the nonlinear Zeeman effect. The observed extremal cross-sectional area is given by the extrapolation of $dS(B)/dB$ to $B = 0$, yielding $S_{\text{up}}^{\text{obs}} \neq S_{\text{down}}^{\text{obs}}$.

as shown in figure 4(e), and the γ orbit with $F_\gamma \sim 690$ T is comparable to the frequency associated with the cross-shaped electron pockets around the X points [figure 4(f)].

However, there are important discrepancies between the theoretical results and the measured dHvA frequencies: angle-dependent branches and branches with frequencies less than about 40 T are absent in the measured data, and the measured frequencies exhibit slight splitting, which is absent in the theoretical ones. We observe nearly isotropic angular dependence of dHvA frequencies, and the splittings of frequencies are also isotropic. In the δ orbit, the observed splitting is $\Delta F_\delta^{\text{obs}} \sim 45$ T, but the theoretical calculations predict no splitting in the branch near ~ 2900 T. In the β and γ orbits, the observed splittings are $\Delta F_\beta^{\text{obs}} \sim 40$ T and $\Delta F_\gamma^{\text{obs}} \sim 70$ T. However, the theoretical calculations indicate that the frequencies for the β' and γ' orbits, stemming from the triangle-shaped and cross-shaped electron pockets [figures 4(e) and (f)], respectively, depend strongly on the angle θ as shown in figure 3(c), yielding angular dependent splitting in the oscillation frequencies. Moreover, the splittings of calculated frequencies $\Delta F_\beta^{\text{calc}} = F_{\beta'}^{\text{calc}} - F_\beta^{\text{calc}} = 150$ T at $\theta = 45^\circ$ and $\Delta F_\gamma^{\text{calc}} = F_{\gamma'}^{\text{calc}} - F_\gamma^{\text{calc}} = 1200$ T at $\theta = 0^\circ$ and 90° are much larger than the observed $\Delta F_\beta^{\text{obs}}$ and $\Delta F_\gamma^{\text{obs}}$. We therefore conclude that the experimentally detected β and γ orbits represent only parts of the corresponding theoretical orbits. The absence of these angle-dependent branches in our measurements can be attributed to the suppression of oscillation amplitudes by the large curvature factor $\Delta\tau \propto |\partial^2 S(k)/\partial k_\parallel^2|^{-1/2}$, suggested by the shape of calculated Fermi surfaces.

The slight splitting of oscillation frequencies observed in CaSn_3 is reminiscent of the spin splitting of energy bands. For instance, in noncentrosymmetric systems with strong SOC, asymmetric SOC can induce the splitting of Fermi surfaces even in the absence of a magnetic field [5, 20]. However, since CaSn_3 is a centrosymmetric system, asymmetric SOC

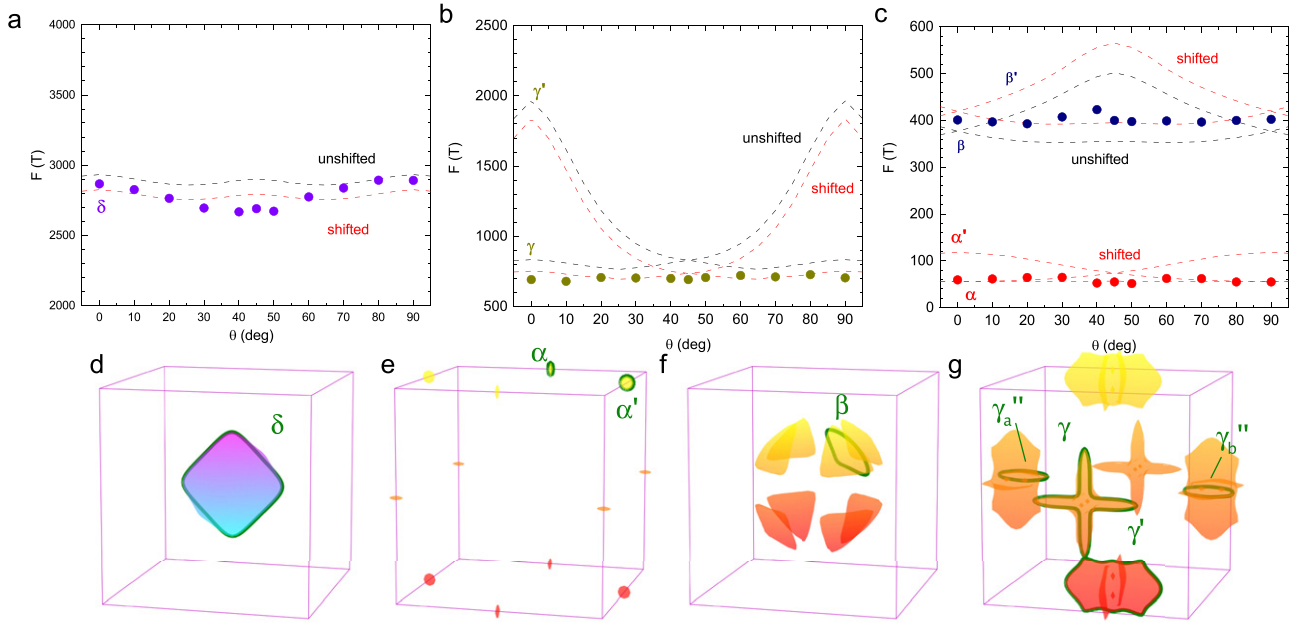


Figure 6. Comparison between experimental and calculated dHvA frequencies. Angular dependence of average dHvA frequencies for (a) the δ orbit, (b) the γ orbit, and (c) the α and β orbits. Black and red dashed lines represent theoretical dHvA frequencies without and with Fermi-energy shifts, respectively. Fermi surfaces with shifting the Fermi energy by (d) +40 meV for the hole band around the Γ point, (e) +110 meV for electron pockets around the M points, (f) +15 meV for electron pockets located between the R and Γ points, and -20 meV for electron pockets around the X points. Green lines represent extremal orbits when the field is applied parallel to the $[100]$ axis.

is absent. Instead, the observed splitting in CaSn_3 can be attributed to spin-up and down Fermi surfaces with field-dependent extremal cross sectional areas $S(B)$ due to the Zeeman effect. Taking the Zeeman effect into account, the Onsager relation can be rewritten as $F = \hbar(S(B) - BdS(B)/dB)/(2\pi e)$. Hence, the measured F represents a back projection of field-dependent cross-sectional area $S(B)$, i.e. an extrapolation of the tangent at B to $B = 0$ (figure 5) [21–24]. In the conventional linear Zeeman effect, the back projection provides field-independent $S^{\text{obs}} = S(0)$, or field-independent dHvA frequencies F^{obs} [figure 5(a)]. In this case, the observed frequencies for spin-up and down Fermi surfaces are identical ($F_{\text{up}}^{\text{obs}} = F_{\text{down}}^{\text{obs}}$). On the other hand, the nonlinear Zeeman effect can give rise to nonlinear magnetic field dependence of extremal areas $S_{\text{up}}(B)$ and $S_{\text{down}}(B)$, yielding the disparity between the observed extremal areas $S_{\text{up}}^{\text{obs}}$ and $S_{\text{down}}^{\text{obs}}$, i.e. $F_{\text{up}}^{\text{obs}} \neq F_{\text{down}}^{\text{obs}}$ [figure 5(b)]. In this situation, averaging two splitting frequencies provides the zero-field limit for each orbit: $F_{\alpha}^{\text{ave}} = 60$ T, $F_{\beta}^{\text{ave}} = 401$ T, $F_{\gamma}^{\text{ave}} = 692$ T, and $F_{\delta}^{\text{ave}} = 2868$ T. Shifting the Fermi energy upward by 15 meV for the β orbit, downward by 20 meV for the γ and γ' orbits, and upward by 40 meV for the δ orbit fully reproduce their absolute frequencies [figures 6(a)–(c)]. Field-dependent dHvA frequencies for spin-up and down Fermi surfaces have also been reported for PrPb_3 with the same AuCu_3 -type cubic structure [25].

Whereas the Fermi pockets corresponding to the measured orbits β , γ , and δ are uniquely identified, the α orbit with $F_{\alpha}^{\text{ave}} = 60$ T remains unassigned. We note that the hole pocket around the Γ point and triangle-shaped electron pockets between Γ and R points provide no extremal orbits other than $F \sim 3000$ T and ~ 400 T at $\theta = 0$, respectively [figures 4(d),

(e) and 6(d), (f)]. On the other hand, the cross-shaped electron pockets around the X points has extra extremal orbits γ'' with the frequency of ~ 190 T (150 T) for the unshifted (shifted) Fermi pockets [figures 4(f) and 6(g)] at $\theta = 0$. Since the calculated frequencies for the γ'' orbit, with or without the Fermi-energy shift, are larger by a factor of ~ 3 than the measured frequency of 60 T, the α orbit cannot be ascribed to the cross-shaped electron pockets.

Thus, we have two possible options to assign the α orbit: tiny hole pockets around the large Fermi surface at the Γ point and tiny electron pockets at the M points. However, the isotropy of the dHvA frequencies for the α orbit suggests that it is quite unlikely that the α orbit originates from the small non-spherical hole pockets located off the high symmetry points in band 25. The absence of these tiny hole pockets can be due to the sensitivity of the pocket sizes to the Fermi energy, as figure 4(a) suggests.

We therefore attribute the α orbit to the electron pockets around the M points. In the band structure with the unshifted Fermi energy, however, the cross sectional areas of the electron pockets around the M points are very small [figure 4(c)]. Nevertheless, as shown in the calculated band structure [figure 4(a)], the sizes of the electron pockets are extremely sensitive to the Fermi energy E_F . Indeed, an upward shift of E_F by 110 meV yields perfect agreement in the absolute frequency and its angular dependence [figure 6(c)] just like the other Fermi pockets in CaSn_3 . This assignment to the α orbit, with a shifted Fermi energy, leads to the intriguing conclusion that three TRIM—namely, the Γ , X , and M points—are surrounded by the Fermi pockets of CaSn_3 , which satisfies

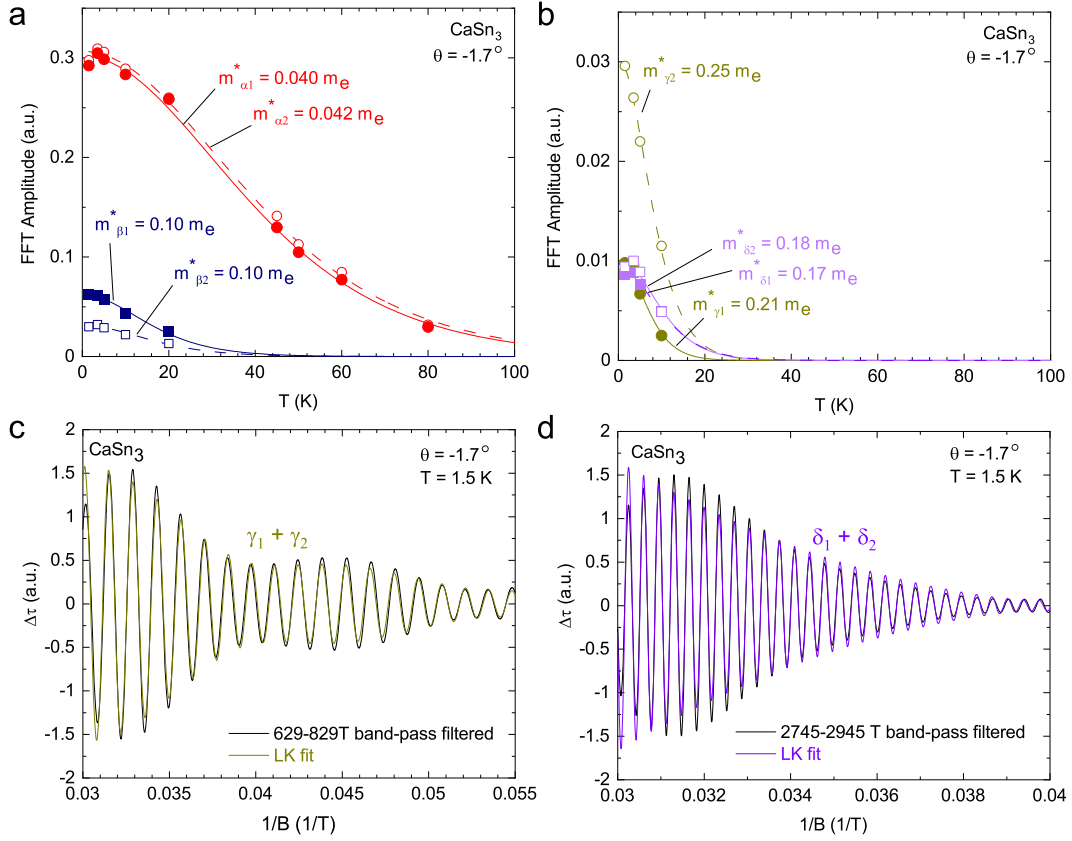


Figure 7. Effective masses and Berry phases of CaSn₃. Effective masses of (a) the α and β orbits and (b) the γ and δ orbits in CaSn₃, obtained from temperature dependence of FFT amplitudes at $\theta = -1.7^\circ$ [figure 2(a)] using the Lifshitz–Kosevich (LK) model with the average inverse field $1/\bar{B} = (1/B_{\min} + 1/B_{\max})/2$, where $B_{\min} = 5$ T and $B_{\max} = 35$ T. A two component LK fit to the band-pass filtered data for (c) the γ and (d) the δ orbits. The extracted Berry phase $\phi_B = -0.7\pi$ for the γ orbit and 1.0π for the δ orbit—indicate nontrivial topological nature of CaSn₃.

one of the criteria theoretically proposed for the realization of topological superconductivity.

3.3. Effective masses and Berry phases

To take a closer look at the effective mass and topological nature of each band, we utilize the LK model that explains the oscillatory part of magnetic torque in metals [21],

$$\Delta\tau^{\text{osc}} = M_{\perp}^{\text{osc}} \times B, \quad (1)$$

$$M_{\perp}^{\text{osc}} = -\frac{1}{F} \frac{dF}{d\theta} M_{\parallel}^{\text{osc}}, \quad (2)$$

$$M_{\parallel}^{\text{osc}} \propto -B^{\frac{1}{2}} \left| \frac{\partial^2 S(k)}{\partial k_{\parallel}^2} \right|^{-\frac{1}{2}} R_T R_D \sin \left[2\pi \left(\frac{F}{B} + \phi^{\sigma} \right) \right]. \quad (3)$$

Here, $R_T = x/\sinh x$ —with $x = am^*T/m_eB$ and $a = 2\pi^2k_B m_e/e\hbar = 14.69$ T K⁻¹—is the thermal damping factor, $R_D = \exp(-am^*T_D/m_eB)$ is the Dingle damping factor, m^* is the carrier effective mass, m_e is the free electron mass, and T_D is the Dingle temperature. The phase shift ϕ^{σ} ($\sigma = \text{up, down}$) for a spin-up/down Fermi surface is given by $\phi^{\sigma} = -1/2 + \phi_B^{\sigma}/2\pi \pm \phi_Z^{\sigma}/2 + \phi_{3D}$, where ϕ_B^{σ} is the Berry phase and $\phi_Z^{\sigma} = gm^*/2m_e$ (g : g-factor) is a phase shift due to the linear Zeeman effect.

The phase shift determined by dimensionality of the Fermi surface, ϕ_{3D} , is $1/8$ for extreme minima (maxima) for electron (hole) pockets and $-1/8$ for extreme maxima (minima) for electron (hole) pockets. Note here that instead of using the spin damping factor $R_S = \cos(\pi gm^*/2m_e)$ in the conventional LK formula, we adopt the Zeeman phase shift ϕ_Z^{σ} to describe the effect of spins due to the spin-dependent dHvA frequencies ($F_{\text{up}} \neq F_{\text{down}}$). To extract a reliable Berry phase from dHvA oscillations, ϕ_Z^{σ} , together with the sign of $dF/d\theta$, should be considered in the LK analysis.

To this goal, we first determine the effective masses m^* through the thermal damping factor R_T by fitting the observed FFT amplitudes to the LK formula [21]. We find the effective masses m^* are $0.040m_e$, $0.042m_e$, $0.10m_e$, $0.10m_e$, $0.21m_e$, $0.25m_e$, $0.17m_e$, and $0.18m_e$ for the α_1 , α_2 , β_1 , β_2 , γ_1 , γ_2 , δ_1 , and δ_2 orbits, respectively [figures 7(a) and (b)]. These light masses are consistent with the previously reported values [10].

Nontrivial topological nature of CaSn₃ is confirmed by the nonzero Berry phase. To determine the Berry phase, we fit a two-component LK formula to band-pass filtered data for the γ and δ orbits for $\theta = -1.7^\circ$ at $T = 1.5$ K. We use the oscillation frequencies obtained from the FFT analysis and the effective masses extracted from the temperature dependence of FFT amplitudes as fixed parameters. We assume that the

spin-up and down Fermi surfaces have the same Berry phase, i.e. $\phi_B = \phi_B^{\text{up}} = \phi_B^{\text{down}}$. Taking into account the signs of $dF/d\theta$ (< 0 around $\theta = 0$) for the γ and δ orbits [figures 6(a) and (b)], we find the extracted Berry phases $\phi_B = 0.7\pi$ for the γ orbit and $\phi_B = 1.0\pi$ for the δ orbit, which indicate the non-trivial topological nature of these bands. The lower limits of effective g -factors, obtained from the Zeeman phase shift, are 8.61 for the γ orbit and 11.6 for the δ orbit. Similar, sizable enhancement of g has been observed in various topological semimetals, including ZrSiS [26], ZrTe₅ [27], Cd₃As₂ [28], and PtBi_{2-x} [29], all consistent with the large Zeeman splitting.

4. Conclusions

In summary, we have observed four fundamental dHvA oscillation frequencies in CaSn₃ via torque magnetometry in magnetic fields up to 35 T, determined to be $F_{\alpha}^{\text{ave}} = 60$ T, $F_{\beta}^{\text{ave}} = 401$ T, $F_{\gamma}^{\text{ave}} = 692$ T, and $F_{\delta}^{\text{ave}} = 2868$ T. We have identified the correspondence between the experimental quantum oscillation frequencies and theoretically calculated orbits in this topological superconductor candidate, revealing that an odd number of Fermi pockets enclose the TRIM, prerequisite to one of the theoretical criteria for topological superconductivity. The nonzero Berry phases are also confirmed by using the LK model, supporting the nontrivial topological nature of this system. These findings provide a new avenue to investigate topological superconducting states stabilized in topological semimetals.

Data availability statement

The data that support the findings of this study are available upon reasonable request from the authors.

Acknowledgments

The authors thank Hiroaki Shishido for helpful discussions. The experimental work was supported in part by the start-up fund from the University of Central Florida. HS and YN were supported by NSF CAREER DMR-1944975, and XH and YT by the NHMFL UCGP program. Theoretical work (DL and TSR) was supported by DOE Grant DE-FG02-07ER46354. The NHMFL is supported by the National Science Foundation through NSF/DMR-1644779 and the State of Florida.

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