# Progress Towards a Higher Sensitivity <sup>13</sup>C-Optimized 1.5 mm HTS NMR Probe

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Abstract-Nuclear magnetic resonance (NMR) probes using thin-film high temperature superconducting (HTS) resonators offer high sensitivity and are particularly suitable for small-sample applications. We are developing an improved 1.5 mm HTS NMR probe designed for operation at 14.1 T and optimized for <sup>13</sup>C detection. The total sample volume is about 35  $\mu L$  and the active sample volume is 20  $\mu$ L. The probe employs HTS resonators for <sup>13</sup>C and <sup>1</sup>H transmission and detection and the <sup>2</sup>H lock. We examine the interactions of multiple superconducting resonators and normal metal tuning loops on coil resonance frequency and probe sensitivity. We test a recently introduced <sup>13</sup>C resonator design, engineered to significantly increase <sup>13</sup>C detection sensitivity over previous all-HTS probes. At zero field, we observe a <sup>13</sup>C quality factor of 6000 which is several times higher than previous resonators. In this work the coil design considerations and probe build-out procedure are discussed.

*Index Terms*—Nuclear magnetic resonance, high-temperature superconductors, superconducting devices.

#### I. INTRODUCTION

**N** UCLEAR magnetic resonance (NMR) is a powerful molecular characterization technique useful for the study of solution samples in biology, biochemistry, and organic chemistry. <sup>13</sup>C detection provides direct information concerning the carbon scaffolding that forms biological molecules and is ideal for natural products chemistry and metabolomics applications. However, <sup>13</sup>C NMR suffers from low sensitivity because of its 1.1% natural abundance and low gyromagnetic ratio [1]. Enhancing the sensitivity on an NMR probe can be effectively

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accomplished by improving the signal-to-noise ratio (SNR) of the NMR probe. The SNR of a probe for a given sample can be described by

SNR 
$$\propto \frac{M_0 B_1 / I_{\text{coil}}}{[(T_a + T_s) R_s + (T_a + T_{\text{coil}}) R_{\text{coil}}] 1/2}$$
 (1)

where  $M_0$  is the sample magnetization,  $B_1/I$  is the strength of the RF excitation pulse per unit current in the coil,  $T_{coil}$ ,  $T_{a}$ , and  $T_{\rm s}$  are the coil, preamplifier and sample noise temperatures, respectively, and  $R_{\rm s}$  and  $R_{\rm coil}$  are the effective resistance of the sample and coil, respectively [2]. Thin-film high temperature superconducting (HTS) resonators improve SNR by reducing coil resistance  $R_{coil}$  beyond what can be achieved with a normal metal coil [3]-[6]. We report here the design, construction, and rf measurements of an improved 1.5 mm<sup>13</sup>C-optimized all-HTS NMR probe. A 1.5 mm<sup>13</sup>C-optimized all-HTS probe [1] of similar design (including a <sup>15</sup>N channel) previously developed in our lab has shown to be a powerful tool for metabolomics applications [7]–[11]. Although the previous probe achieved the highest <sup>13</sup>C mass sensitivity of any solution NMR probe when it was introduced, it did not realize the full potential of using HTS coils (mass sensitivity in NMR is defined as the SNR of a standard measurement divided by the volume of sample used for the measurement). Advances in probe construction technique and coil design are expected to produce significant improvements in <sup>13</sup>C detection sensitivity over the previous probe. Also, by employing an effective model of inter-probe resonator interactions to inform resonance frequency adjustments, the efficiency of the probe build-out process was improved [12].

## II. PROBE DESIGN

The <sup>13</sup>C optimized 1.5 mm all-HTS probe in development was designed for a nominally 600 MHz NMR spectrometer. The total sample fill volume is about 35  $\mu$ l and active sample volume is 20  $\mu$ l. The probe features <sup>13</sup>C and <sup>1</sup>H detection channels and a <sup>2</sup>H lock system which ensures the spectrometer operates at a constant net magnetic field [13]. At the magnet's field of 14.1 T, isotopes <sup>13</sup>C, <sup>1</sup>H, and <sup>2</sup>H have Larmor frequencies of 150.8 MHz, 599.7 MHz, and 92.1 MHz, respectively. The cryogenic probe body features three pairs of HTS coils mounted in a Helmholtz-like configuration with coupled resonances at the Larmor frequencies of <sup>13</sup>C, <sup>1</sup>H and <sup>2</sup>H (Fig. 1). Each of the six individual coils was patterned by Star Cryoelectronics (Santa Fe, NM, USA) from ~300 nm-thick films of Y<sub>1</sub>Ba<sub>2</sub>Cu<sub>3</sub>O<sub>7- $\delta$ </sub> (YBCO) coated epitaxially onto 430  $\mu$ m-thick sapphire substrates by Ceraco, GmBH (Ismaning, Germany). The probe-head

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Fig. 1. Design of the 1.5-mm all-HTS NMR probe. Some details and dimensions are simplified or distorted for illustrative purposes and are not exact reproductions of the design. (a) Diagram of the NMR probe-head illustrating the arrangement of two pairs of HTS coils and the corresponding normal metal power-matching and tuning loops. (b) Cross-sectional schematic of the coil arrangement. Three Helmholtz-like pairs are maintained under vacuum at 35 K and surround the 1.5-mm sample tube.

was maintained at vacuum and cooled using a Varian cryogenic system to 35 K, well under the superconducting transition temperature of YBCO (93 K). To inductively couple energy into the coil pairs, three movable coaxial cables terminated into normal-metal loops were adjusted to minimize the reflection coefficient  $S_{11}$  at the relevant modes. A vector network analyzer (VNA) was used to measure the reflected response in continuous wave (CW) mode at 0 dBm incident power, which is below the non-linearity threshold of the HTS coils [14]. Three shorted inductive normal-metal tuning loops were employed to give users the ability to finely tune probe resonances to the exact Larmor frequencies of the nuclei intended for detection during routine probe use [1], [3], [15], [16].

#### A. Coil Designs

To maximize sensitivity, the <sup>13</sup>C detection coils were placed closest to the sample. Counter-wound spiral resonator designs were employed for the <sup>13</sup>C resonators (Fig. 2(a)). This design is useful for the innermost coils because the large stray electric field usually associated with low frequency spiral coils is trapped within the sapphire between two spirals [1], [17]. The first iteration of the probe employed two single-sided spiral resonators glued back-to-back [17]. Such a configuration reduced the filling factor of the probe due to the doubled substrate thickness. The current <sup>13</sup>C coil design utilizes double-side coated wafers to improve filling factor [18]. Two 4-turn spiral YBCO structures with opposite handedness were coated onto either side of the sapphire substrate.

To minimize the effect of the diamagnetism of the superconductor on the static magnetic field and improve lineshape, the 144.5  $\mu$ m spiral traces of the <sup>13</sup>C spiral resonators were slit into 14 fine parallel "fingerlets", each 8  $\mu$ m wide and separated by 2.5  $\mu$ m (Fig. 2(a)) [19]. This minorly affected the rf performance of the coil but is expected to reduce magnetization effects by a factor of approximately 14 [20]. This also allowed the current in adjacent fingerlets to flow in opposite directions, causing each spiral mode to split into a family of modelets. Many of these spurious modes were too close to the <sup>1</sup>H Larmor frequency (600 MHz in our case) and would interfere with <sup>1</sup>H



Fig. 2. Design of the  $^{13}$ C detection coils. (a) Pair of counter-wound spiral resonators. Each resonator employs two 4-turn YBCO spiral structures with opposite handedness coated onto either side of a sapphire substrate. To reduce magnetization, the HTS resonators are slit into 14 fine parallel fingerlets. The slits cause each mode to split into a family of modelets. (b) The modelets of one single-sided spiral coil as simulated using IE3D.



Fig. 3. Simulated modes of our current counter-wound (CW) spiral  $^{13}$ C detection coils. The modelets of the slit single spiral coil show further splitting when they are used in a CW spiral arrangement. Our simulation shows only a single mode near the <sup>1</sup>H resonance of 600 MHz.

detection. In the previous design, a gold overlayer was employed to suppress the modelets [21]. While this normal-metal overlayer was successful in suppressing the modelets, it also significantly increased the loss of the resonator. Thus, the sensitivity of the <sup>13</sup>C channel was reduced. Removing this gold layer was our main design goal for the new <sup>13</sup>C detection coils.

The EM simulation program IE3D (Mentor Graphics) was used to assist in the design of the <sup>13</sup>C resonator. By simulating the resonance spectra of candidate spiral coil designs in IE3D, we determined that the splitting of modelets follows a consistent pattern (Fig. 2(b)). When the coil is slit into 2 fingerlets, each mode of the spiral splits into 2 modelets. It can be noted that the lower modelet has currents flowing in the same direction in the two fingerlets, whereas in the upper modelet, the currents in the two fingerlets are flowing in opposite directions. Further slitting of the spiral produces more modelets just below the upper modelet of the 1-slit coil. Thus, a relatively simple simulation of the 1-slit counter-wound spiral can be used to know the approximate range of frequencies for the modelets.

Fig. 3 shows the predicted modes of our current counterwound spiral coil. All the modelets of a single spiral show a further splitting when they are used in a counter-wound configuration. As can be seen, we expect to have a family of modelets originating from the fundamental mode of the spiral to resonate well below the <sup>1</sup>H Larmor frequency. Our simulation shows only a single mode near the <sup>1</sup>H resonance. The higher modes of the spiral have very little dipole moment and do not shift appreciably when two counter-wound spiral coils are deployed in a Helmholtz configuration. We expect that this resonance can be easily shifted away during the laser trimming process to adjust the coil frequency. Thus, it was safe to omit the gold overlayer. By contrast, the older version of the coil, if the gold overlayer was omitted would have produced a family of modelets around the <sup>1</sup>H Larmor frequency which cannot be easily shifted away with laser trimming.

The <sup>1</sup>H and <sup>2</sup>H coils employed the same design as in the previous probe of similar design described in [1]. In short, a single-sided interdigital-capacitor based design, known as a racetrack design, with 24 fingers and four gaps was used for the <sup>1</sup>H detection coils [22]. The <sup>2</sup>H detection coils employed a single-sided spiral resonant structure with 10 turns.

## B. Coil Resonance Adjustments

In constructing this probe, we also looked to develop methods to increase the general efficiency of the build-out process of HTS probes. HTS probe construction can be a tedious and time-consuming process, which is part of the reason that HTS coils have yet to be widely implemented in commercial NMR probes. The sensitivity of HTS coils to their local environment is a significant contributor to this difficulty. In multi-channel HTS probes, the coils are packed tightly around the sample and each coil's resonance frequency is appreciably shifted by the presence of the other HTS resonators. The resulting resonances are the coupled resonances of all the resonators, not just the Helmholtz pairs. Additionally, variability in substrate thickness and coil patterning lead to differences in resonance frequency between coils of the same design. Therefore, coil resonance frequencies must be adjusted after fabrication. However, without a model describing coil interactions and resonance shifts the necessary adjustments to each coil are unknown. A build-out procedure generally requires four or more iterative adjustments to each coil to get within the tuning range of the tuning loops, about 1 to 2 percent of the coil resonance frequency.

The magnetic coupling model described in detail in [12] was used to predict the individual coil resonances required for the ensemble of HTS coils to obtain the desired set of coupled modes. We hoped that by modeling only the magnetic coupling we could describe coil interactions with sufficient accuracy to reduce coil adjustment procedures to one to two steps. To adjust the resonance of a coil a 532-nm laser mounted on a microscope probe station was used to eliminate portions of YBCO and increase the resonance of each coil to the desired frequency [23]. To predict what the resonance frequency of a single coil would be after a laser trim, we conducted trimming simulations using the EM simulation tool Sonnet (Sonnet Software, Inc., Syracuse, NY).

An additional problem for laser trimming the new doublesided resonators is the difficulty of trimming one side of the resonator without damaging the opposite side. To address this problem, each side of the <sup>13</sup>C resonator was designed with a non-overlapping half turn. We determined that with a sufficiently small laser beam size one side of the coil could be trimmed without affecting the opposite side.

#### **III. RESULTS AND DISCUSSION**

Much of the influence of a resonator on probe sensitivity can be quantified by the measurement of its quality factor (Q factor or Q), where  $Q \propto R_{coil}^{-1}$ . With the final coil adjustments made and the coupling and tuning loops relatively optimized, the new probe Q factors can now be compared with zero field data from the previous 1.5 mm <sup>13</sup>C-optimized all-HTS probe of similar design. The matched Q factors measured from the -3 dB points of the reflection coefficients of the fully loaded and tuned probe in no external magnetic field are listed in the table below:

Nucleus	F <sub>Larmor</sub> (MHz)	Q <sub>Larmor</sub>
<sup>13</sup> C	150.81	6000
$^{1}\mathrm{H}$	599.69	3900
<sup>2</sup> H	92.06	2100

These Q factors compare very favorably to the zero field Q factors of 1900, 2000, and 1500 for <sup>13</sup>C, <sup>1</sup>H, and <sup>2</sup>H channels, respectively, observed in the previous probe. Notably, the new <sup>13</sup>C coil design exhibits 3.2 times the Q factor. In recent in-field tests, <sup>13</sup>C channel Q is largely preserved since the coil substrate-planes are mounted approximately parallel to the applied magnetic field [24]. We measure a <sup>13</sup>C channel Q factor of 5500 at 14.1 T, compared a Q factor of 1700 in the previous probe. The effects of the normal metal tuning loops on the nearby HTS resonators can be significant and small adjustments in loop position can cause large changes in probe sensitivity. Still more sensitivity can be gained by moving the tuning loop slightly away from the <sup>13</sup>C coils to decrease eddy currents. In zero field tests we have observed a Q of 14000 at the low end of the tuning range where the normal-metal tuning loop minimally couples to the <sup>13</sup>C resonators. However, there are questions as to whether we have the sufficient stability to support such a high Q in this probe body, and more generally if such a high Q is even useful given the  $\sim$ 200 ppm chemical shift dispersion range of <sup>13</sup>C. We may choose to make these sensitivity improvements iteratively rather than all at once.

Since the gold overlayer used in previous  ${}^{13}$ C detection coil designs was omitted in our design, we expected to observe a single mode near the  ${}^{1}$ H resonance of 600 MHz. Experimental results agreed with the IE3D simulations shown in Fig. 3. In single coil tests a single mode was observed at 576 MHz with no nearby modelets. Thus, the new  ${}^{13}$ C coils facilitate a large increase in  ${}^{13}$ C detection sensitivity and do not interfere with hydrogen detection.

Probe sensitivity was improved across all channels even though only <sup>13</sup>C detection coils received a design upgrade. In part, this may be due to the extensive optimizations we made to the size, shape, and position of the inductive tuning loops. We used particularly large <sup>2</sup>H tuning loops located far away from the <sup>2</sup>H resonators to decrease eddy current losses and increased the <sup>2</sup>H channel Q. However, this may not account for the entire 95% and 40% increases in Q observed on the <sup>1</sup>H and <sup>2</sup>H channels when compared to the previous probe. Additional improvements may be attributed to the lack of a <sup>15</sup>N channel in new probe. We established by measuring coupling constants between resonator pairs that pairs that are orthogonal and close in proximity can couple as strongly as Helmholtz pairs [12]. The HTS <sup>15</sup>N detection coils in the old probe were nested exterior to the other three coil pairs and parallel to the <sup>1</sup>H coils [1]. Since the old probe had the same dimensions as the current probe, the <sup>15</sup>N resonators were close in proximity to the <sup>1</sup>H and <sup>2</sup>H resonators. While the <sup>15</sup>N coils were HTS, we can still expect some Q loss. Of more significance was the position of the <sup>1</sup>H normal metal-tuning loop, which needed to be placed in the small gap between the <sup>15</sup>N and <sup>1</sup>H resonators. It was not imperative to place the normal-metal loop so near to the <sup>1</sup>H coils in the new probe. Finally, we may also be observing improvements in HTS film quality on all coils.

The magnetic coupling model was successful in accurately predicting the coupled modes of the probe. Using the measured single coil resonances, the magnetic coupling model allowed us to predict the coupled resonances with a RMSPE of 0.82 [12]. The coupling constants did not change after coil trims. Additionally, implementing accurate trimming simulations using the EM simulation tool Sonnet<sup>TM</sup> enabled the prediction of single coil resonance adjustments via laser trimming with an average error of 0.27%. We calculate that a trimming method which only considered Helmholtz pair resonances would have at best made predictions of the <sup>13</sup>C coupled resonance with  $\sim 2.5\%$  error without considering the effects of other coils. This error is larger than the fine-tuning range of the inductive tuning loops. Furthermore, a "coil spreader" was fitted atop the coil assembly during fully loaded probe measurements. This forced the six coils into a consistent yet unique set of positions when measuring the coupled modes of the full probe. These unique positions were not replicable during experiments where only two coils were measured. Therefore, a coupling model describing the interactions of all six coils is essential in completing trimming within one or two steps.

## IV. CONCLUSION

The new 1.5 mm <sup>13</sup>C-optimized all-HTS NMR probe described here exhibits a significantly better <sup>13</sup>C Q factor which should provide a significant increase in <sup>13</sup>C detection sensitivity. Probe sensitivity was also improved on the <sup>1</sup>H detection channel and the <sup>2</sup>H lock channel. We also demonstrated the substantial effect of normal metal inductive tuning loops on coil Q factors and the importance of accuracy when predicting coupled probe resonances. The application of a magnetic coupling model in conjunction with trimming simulations improved the efficacy of the coil trimming process. The probe has been recently installed in the 600 MHz spectrometer at the University of Florida (UF) and preliminary tests are underway. The remaining in-field tests will be performed at the UF to demonstrate the utility of this probe for <sup>13</sup>C-based metabolomics.

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