

Mott domain walls: A (strongly) non-Fermi liquid state of matterTsung-Han Lee ^{1,2}, J. Vučićević,³ D. Tanasković,³ E. Miranda ⁴, and V. Dobrosavljević ¹¹*Department of Physics and National High Magnetic Field Laboratory, Florida State University, Tallahassee, Florida 32306, USA*²*Physics and Astronomy Department, Rutgers University, Piscataway, New Jersey 08854, USA*³*Institute of Physics Belgrade, University of Belgrade, Pregrevica 118, 11080 Belgrade, Serbia*⁴*Gleb Wataghin Physics Institute, The University of Campinas, Rua Sérgio Buarque de Holanda, 777, CEP 13083-859, Campinas, Brazil*

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Most Mott systems display a low-temperature phase coexistence region around the metal-insulator transition. The domain walls separating the respective phases have very recently been observed displaying unusual properties both in simulations and in experiments. First, they often cover a significant volume fraction, thus cannot be neglected. Second, they resemble neither a typical metal nor a standard insulator, displaying unfamiliar temperature dependence of (local) transport properties. Here we take a closer look at such domain wall matter by examining an appropriate unstable solution of the Hubbard model. We show that transport in this regime is dominated by the emergence of “resilient quasiparticles” displaying strong non-Fermi liquid features, reflecting the quantum-critical fluctuations in the vicinity of the Mott point.

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Introduction. The Mott metal-insulator transition [1,2] remains a subject of much controversy and debate, with disagreement even concerning the physical mechanism [3] that dominates its vicinity. One popular viewpoint [4] regards it as a (strictly) second-order phase transition at $T = 0$, where the dominant degrees of freedom are the intersite spin singlets (e.g. the “spinon” excitations) arising in the vicinity of the Mott insulating state. A complementary dynamical mean-field theory (DMFT) perspective [5] builds on the seminal ideas of Hubbard and Mott, focusing on local Kondo-like processes that govern the condensation [6] of the strongly correlated Fermi liquid on the metallic side. The latter viewpoint predicts that the “evaporation” of the electron liquid at the transition bears some analogy to conventional liquid-gas transitions, with a phase coexistence region arising at low temperatures [5]. While many experiments [7,8] indeed reported the predicted first-order transition within the paramagnetic phase, other experiments [9,10] reported behavior consistent with quantum criticality, which sometimes has been interpreted in terms of the former picture [4].

Resolving this important issue in the context of real materials is further complicated by the emergence of various magnetic, charge, or orbital orders in the vicinity of the Mott point [2], which can often mask the basic underlying mechanism. Recent experimental work, however, has successfully identified [11] a simpler class of model systems, where no broken symmetry phases have been observed anywhere in the phase diagram. This situation is best documented in “spin-liquid” organic materials [12], where careful and precise experiments are starting to paint a clearer picture of the genuine Mott point. Most remarkably, experiments here provided [13] clear evidence for quantum critical scaling [14] of the resistivity curves at intermediate temperatures, with some evidence for a resistivity jump at $T < T_c \sim 30K$, consistent with

the DMFT prediction of a weakly first-order transition [15]. Still, direct evidence of the phase coexistence has emerged only in the recent reports of a colossal enhancement of the dielectric response [16] and the previous near-field infrared imaging [17].

In parallel with the experimental progress, recent theoretical work provided complementary insight into the nature of the metal-insulator coexistence region [18]. Surprisingly “thick” domain walls were observed [19], which are likely to play a central role in governing the observable response in experiments. Indeed, the local transport properties of such domain walls were found [18,19] to display a variety of unusual features, with properties not akin to either those of the conventional metal nor of the insulator. To obtain clear and precise insight into the physical nature of such domain wall matter (DWM), we present in this paper model calculations within the framework of the DMFT picture. We argue that, similarly to conventional Landau theories for domain walls, the *central region* of a domain wall corresponds to a “saddle point” (unstable solution) of the spatially uniform DMFT equations, at the top of the free-energy barrier separating the two competing phases [20,21]. In dramatic contrast to the conventional Landau theory (e.g., for the Ising model), here the two solutions are *not* related by symmetry and display very different physical behavior [22–24]. One is a Fermi liquid metal with coherent quasiparticles (QP) and T^2 resistivity, whereas the other is a Mott insulator with completely incoherent activated transport. What, then, should be the physical properties of the unstable solution separating them? Should it resemble more closely a metal or a Mott insulator? What are the thermal properties of transport in this unfamiliar regime? As a matter of fact, it is almost impossible to guess. Previous studies of the unstable solution were restricted only to the near vicinity of the critical end point ($T \sim T_c$) [25–27], but they did

not provide clear insight as to what happens through the phase coexistence region.

In this paper we present a clear and yet somewhat surprising answer to all these important questions, in a setup which can be considered as a (numerically) exact solution of one of the simplest toy models of strong correlations. Based on a reliable numerical solution of the corresponding DMFT equations we establish that (1) transport in DWM assumes resilient quasiparticle (RQP) character [28,29] throughout the coexistence region; and (2) the relevant RQPs display surprising non-Fermi liquid T -dependence of the QP parameters (see below). These results firmly establish that DWM is a qualitatively different form of matter, which we associate with quantum critical fluctuations around the Mott point.

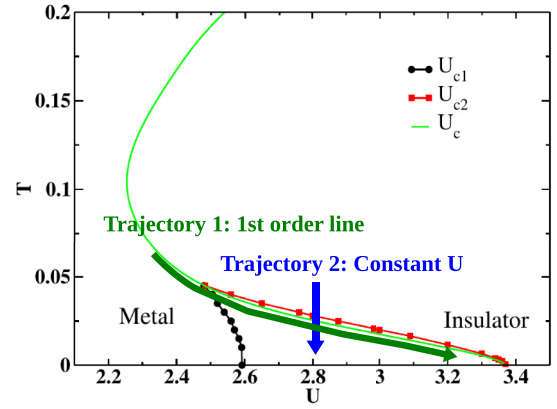
Model calculations. To describe the Mott metal-insulator transition (MIT), while suppressing all forms of magnetic orders, we focus on the maximally frustrated Hubbard model [5,14,30], given by the Hamiltonian,

$$H = - \sum_{\langle i,j \rangle \sigma} t_{ij} (c_{i\sigma}^\dagger c_{j\sigma} + \text{H.c.}) + U \sum_i n_{i\uparrow} n_{i\downarrow}, \quad (1)$$

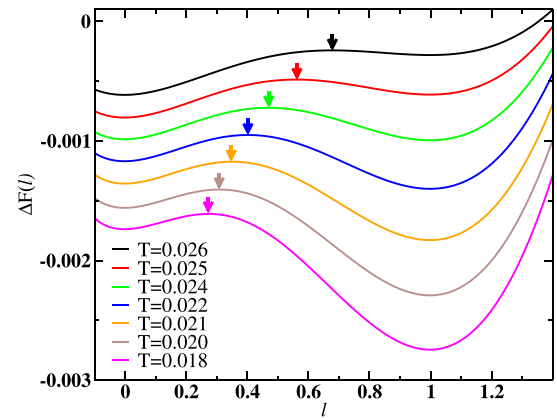
where $c_{i\sigma}^\dagger$ and $c_{i\sigma}$ are the electron creation and annihilation operators, $n_{i\sigma} = c_{i\sigma}^\dagger c_{i\sigma}$, t_{ij} are the hopping elements with zero average and variance $\langle t_{ij}^2 \rangle = t^2 / \sqrt{N}$, and U is the onsite Coulomb potential. The energy unit is set to the half band width, $D = 2t$. Similarly to the popular Sachdev-Ye-Kitaev (SYK) model [31], such an infinite-range model can be exactly solved in the limit where the number of sites $N \rightarrow \infty$. In this case, this is performed through self-consistently solving an Anderson impurity model using the DMFT framework [5]. To solve the impurity problem, we utilize well-known continuous time quantum Monte Carlo (CTQMC) methods as well as iterative perturbation theory (IPT) as impurity solvers [32,33]. The analytical continuation to the real-frequency axis is done using the maximum entropy method (MEM), the fifth-order polynomial fitting for CTQMC, and the Padé approximant for IPT [34,35]. The use of an appropriate N -dimensional optimizer [26] is essential for the convergence to the local saddle point of the free-energy functional (the unstable solution). In addition, an appropriate free-energy analysis [23,36] allows us to identify the first-order transition line, as well as the location of the unstable solution.

The DMFT phase diagram (obtained from IPT), Fig. 1(a), features a second-order critical end point at $T = T_c \sim 0.045$. Below T_c , there emerges a phase coexistence region confined by two spinodal lines $U_{c1}(T)$ and $U_{c2}(T)$, marking the respective instabilities of the Mott insulator and the metallic solutions. At $T = 0$, the first-order transition line merges with the spinodal line $U_{c2}(T)$, and the insulating solution becomes marginally unstable exactly at $T = 0$ [36]. Above T_c , $U_{c1}(T)$ and $U_{c2}(T)$ merge to form a single Widom line, determined from the minimum of the Landau free energy [14].

Finding the unstable solution. In order to understand the behavior of all three solutions of our DMFT theory (metal, insulator, and unstable), we employ the Landau free-energy functional method [23,36], which provides information about the form of the free-energy landscape. Within DMFT, the free energy can be considered as a functional of the local Green function, $G(i\omega_n)$, which for our model assumes the



(a)



(b)

FIG. 1. (a) DMFT phase diagram for the half-filled Hubbard model and the trajectories studied (see text). (b) Evolution of the free-energy functional [36] as T varies for the fixed- U trajectory ($U = 2.83$). Here $l = 0$ and $l = 1$ correspond to the insulating and metallic solutions, respectively. The arrows mark the position of the unstable solutions.

form $F[G] = F_{\text{imp}}[G] - t^2 T \sum_n G^2(i\omega_n)$, where $F_{\text{imp}}[G]$ is the free-energy functional of the associated impurity problem. When solving the DMFT equations by the standard iteration method, one finds convergence [36] to a given local minimum of the free-energy functional, depending on the initial guess for $G(i\omega_n)$. Within the coexistence region, two stable solutions separated by the unstable solution (saddle point) are found. To illustrate this, we follow a “phase space path” [36] connecting the two solutions, which can be parameterized as $G(l) = (1-l)G_{\text{ins}}(i\omega) + lG_{\text{metal}}(i\omega)$ with a parameter $l \in [0, 1]$. The corresponding variation of the free energy can be calculated [36] by evaluating the line integral $\Delta F(l) = t^2 T \int_0^l dl' e_l \cdot \delta G[G(l')]$, where $e_l = (G_{\text{ins}} - G_{\text{met}}) / |G_{\text{ins}} - G_{\text{met}}|$ and $\delta G = G_{\text{imp}}(G) - G$. Here, the dot product denotes a trace over Matsubara frequencies and G_{imp} is the impurity Green function dependent on the initial condition of G .

The unstable solution we seek exists anywhere within the phase coexistence region. To be concrete, however, we examine its evolution following two specific trajectories: (1) along the first-order transition line (where the two stable solutions

have the same free energy); and (2) a trajectory where we vary T at constant U , Fig. 1(a). For illustration, in Fig. 1(b) we follow Ref. [36] and plot the free energy along trajectory (2) (constant U). Here we observe how the unstable solution shifts towards the insulating solution as we lower the temperature and finally merges with the insulating solution at $T = 0$. This confirms that the insulating solution becomes unstable precisely at $T = 0$ throughout the phase coexistence region.

To be able to precisely converge to the desired unstable solution, we should keep in mind that the standard iterative method (essentially a “steepest descent” method) can only find local minima of the free energy, i.e., only the stable solutions. Instead, we use the Broyden method, which can converge to any *extremum* of a given functional (including saddle points) [26], if the initial guess is sufficiently close to the given extremum. Indeed, we find that this method can efficiently converge even to the unstable solution within only a moderate number of iterations. We should stress that the unstable solution found in this way is generally not restricted to lie exactly on the phase space path connecting the two stable solutions, except very close to $T = T_c$. Still, Broyden-converging to the proper unstable solution is greatly facilitated by using the phase space path to estimate an appropriate initial guess for the root search.

Resistivity calculations and quasiparticle transport. To study the transport properties, we utilize the Kubo formula [29] for the DMFT-based DC conductivity,

$$\sigma = \sigma_0 \int d\epsilon \Phi(\omega) \int d\omega \left(-\frac{\partial f(\omega)}{\partial \omega} \right) A(\epsilon, \omega)^2, \quad (2)$$

where the spectral function $A(\epsilon, \omega) = -(1/\pi) \text{Im}[\omega + \mu - \epsilon - \Sigma(\omega)]^{-1}$, $\Phi(\omega) = \Phi(0)[1 - (\omega/D)^2]^{3/2}$, $\sigma_0 = 2\pi e^2/\hbar$, and $f(\omega)$ is the Fermi distribution function. Here $\Sigma(\omega)$ is obtained on the real axis using standard MEM for CTQMC and the Padé approximant for IPT. The resistivity is $\rho = 1/\sigma$. To normalize the resistivity, we use the Mott-Ioffe-Regel (MIR) limit $\rho_{\text{MIR}} = \hbar D/e^2 \Phi(0)$, which represents the scale where the scattering process becomes incoherent and the mean free path is comparable to the Fermi wavelength.

The resistivity calculation, based on Eq. (2), dramatically simplifies in the quasiparticle regime [28], where transport is dominated by only the leading low-energy excitations. Here the Green function can be approximated as $G(\omega, \epsilon) \simeq \frac{Z}{\omega - Z\epsilon + i\Gamma_{QP}}$, with the quasiparticle weight $Z = (1 - \frac{\partial \text{Re}\Sigma(\omega)}{\partial \omega})_{\omega=0}^{-1}$ and scattering rate $\Gamma_{QP} = -Z \text{Im}\Sigma(\omega=0)$. A further Sommerfeld approximation can be performed in situations where $\Gamma_{QP} < T$ and $T < ZD$, and the conductivity can be expressed in terms of only two parameters: Z and $\Gamma = \Gamma_{QP}/Z$, viz.,

$$\frac{\sigma}{\sigma_{\text{MIR}}} \approx \frac{1}{\Gamma} \tanh\left(\frac{Z}{2T}\right). \quad (3)$$

We explicitly checked that these conditions are indeed obeyed throughout the coexistence region, not only by our metallic solution, but also by the unstable solution. As we explicitly show below, the results obtained from numerically evaluating the conductivity using our full DMFT solution and Eq. (2) demonstrate remarkable qualitative and even semiquantitative agreement with our QP approximation. This important

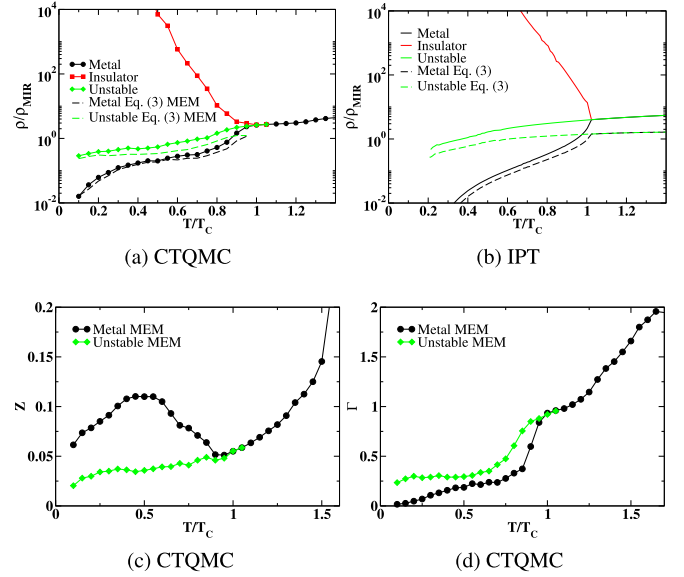


FIG. 2. The resistivity for the metallic (black circles), insulating (red squares), and unstable (green squares) solutions along the first-order transition line in a logarithmic ρ scale for (a) CTQMC and (b) IPT. The Sommerfeld approximations to the resistivities [Eq. (3)] are shown in the corresponding dashed and dotted lines with different analytic continuation methods (MEM for CTQMC and Padé approximant for IPT). (c) The quasiparticle weight Z for the metallic and unstable solutions analytic continued by MEM (black and green symbols). (d) The scattering rate Γ , for the metallic and the unstable solutions, obtained from MEM (black and green symbols).

result demonstrates the resilient quasiparticle character [29] of transport even for our unstable solution, despite the very unusual behavior of the QP parameters in question.

Following the first-order transition line. To investigate how our three solutions evolve when approaching the zero-temperature critical point $U_{c2}(T=0)$, we study the transport properties along the first-order transition line connecting the two critical points, $U_c(T=T_c)$ and $U_{c2}(T=0)$. In Figs. 2(a) and 2(b) we show the results obtained from CTQMC and IPT, respectively. At the critical end point $T = T_c$, the three solutions merge as expected, and the resistivity is of the order of the MIR limit. Below T_c , the three solutions trifurcate into different trajectories. The unstable solution (green diamonds) displays higher resistivity than the metallic solution (black circles), with values of the order of the MIR limit, $\rho \sim \rho_{\text{MIR}}$, indicating bad metal behavior [37]. The insulating solution has much higher resistivity due to standard activated transport.

Close to the zero-temperature critical point $U_{c2}(T=0)$ the three solutions do not merge, in contrast to the situation around the critical end point ($T \sim T_c$). Instead, while the resistivity of the metallic solution drops at low temperatures, that of the unstable solution remains comparable to the MIR limit, suggesting incoherent transport, despite these trends being well captured by the QP approximation [see Figs. 2(a) and 2(b)]. To better understand this behavior, in Fig. 2(c) we show the quasiparticle weight Z for the unstable (green diamonds) and metallic (black circles) solutions. The unstable solution has significantly lower Z than the metal, displaying

a more pronounced decrease at low temperatures, reminiscent of resilient quasiparticles [29]. Note that the increase followed by the decrease of Z in the metallic solution may be attributed to the position of the first-order transition line in the coexistence region, which shifts towards the insulating phase with lowering the temperature. Similar behavior is seen in Fig. 2(d), where we display the behavior of the scattering rate Γ , which for the unstable solution (green diamonds) remains appreciable down to the lowest temperatures, again signaling poorly developed (resilient) quasiparticles. Remarkably, such non-Fermi Liquid (NFL) behavior here persists down to the lowest temperatures, in contrast to previously identified examples of RQPs [29], which emerged only at temperatures intermediate between the conventional Fermi liquid metal at the lowest T and a fully incoherent conductor at high T .

Constant U trajectory. In order to further understand the behavior of the unstable solution in the entire coexistence regime, we also study the resistivity as a function of T along a constant U trajectory. From the free-energy analysis, Fig. 1(b), we anticipate that the unstable solution gradually shifts towards the insulator as T is reduced at fixed U , eventually merging with it at $T = 0$. In contrast, in Figs. 3(a) and 3(b), we observe the metallic and insulating solutions displaying conventional Fermi liquid and activated behaviors, respectively. On the other hand, for the unstable solution, we find that the resistivity (green diamonds) increases as the temperature decreases, reaching values as much as two orders of magnitude larger than the MIR limit. Nevertheless, as shown in Figs. 3(c) and 3(d), we observe that the unstable solution's density of states (DOS) at the lowest temperature still features a very small quasiparticle peak at the Fermi level. This suggests that the unstable solution still retains some metallic character, even though the resistivity is much larger than the MIR limit. In some sense, this situation could be characterized as an extreme example of bad metal (BM) behavior [37], albeit in a setup which is dramatically different than the familiar high- T BM behavior in correlated matter. And indeed, the standard RQP-Sommerfeld approximation again captures remarkably well all the transport trends, even in this extreme high-resistivity regime.

To even more precisely characterize such RQP-NFL behavior, we next examine the corresponding QP parameters and their evolution as a function of T . In Fig. 3(e) we show the quasiparticle weight for Z for metallic (black circles) and unstable (green diamonds) solutions. The metal has a normal behavior with Z saturating at low temperatures, consistent with the expected FL behavior. In dramatic contrast, Z corresponding to the unstable solution decreases rapidly with temperature, displaying power-law behavior $Z \sim T^2$. Remarkably, a similar but much weaker decrease of the form $Z \sim 1/|\log T|$, dubbed a ‘marginal Fermi liquid’ (MFL) [38], was proposed as the key signature of the breakdown of Fermi liquid theory in optimally doped cuprates. The behavior found here is not even marginal. By analogy, it can be described as ‘fully developed NFL’ behavior, the like of which is seldom seen in correlated matter. Analogously, the unstable solution's scattering rate *increases* at low temperatures [Fig. 3(f)], again in power-law fashion $\Gamma \sim 1/T^2$, well exceeding the MIR limit and consistent with transport.

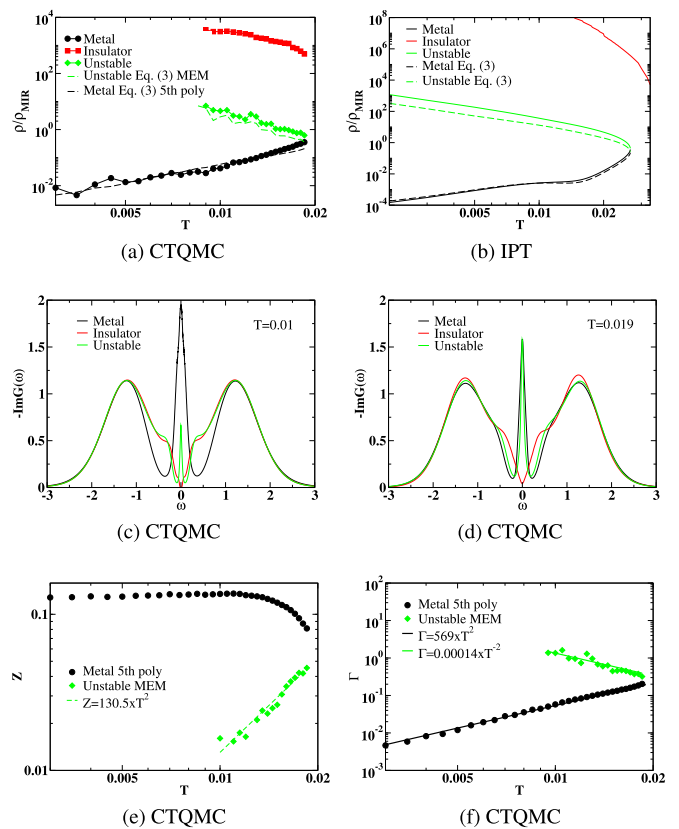


FIG. 3. The resistivity for the metallic (black circles), insulating (red squares), and unstable (green diamonds) solutions along the constant U trajectory in logarithmic ρ scale for (a) CTQMC and (b) IPT. The Sommerfeld approximations to the resistivities [Eq. (3)] are shown in the corresponding dashed and dotted lines with different analytic continuation methods (MEM and polynomial fitting for CTQMC and Padé approximant for IPT). The density of states at low temperatures (c) $T = 0.01$ and (d) $T = 0.019$ near the spinodal line U_{c2} computed from the CTQMC impurity solver and MEM analytic continuation. (e) The quasiparticle weight Z for the metallic and the unstable solutions. (f) The scattering rate Γ for the metallic and the unstable solutions.

Conclusions. In this paper, we identified what may be a new state of correlated electronic matter, characterizing the domain walls within the metal-insulator coexistence region around the Mott point. We showed that its low-energy excitations display a number of unusual properties which qualitatively differ from either a conventional metal or an insulator. This paints a physical picture of exotic quasiparticles barely persisting at the brink of an insulating state. Conceptually, such non-Fermi liquid behavior can be viewed as reflecting the quantum critical fluctuations associated with the metal-insulator transition region.

Our solution was obtained within the framework of single-site DMFT theory, which physically represents the limit of large frustration, where all possible symmetry-breaking fluctuations are suppressed. The MIT coexistence region, however, is presently known [16] to persist in real physical systems such as quasi-two-dimensional Mott organics, where intersite spin correlations could also play a role [39]. The

effects of such perturbations can be systematically studied within cluster-DMFT theories [36,40], with indications that the phase coexistence region can be significantly influenced. Nevertheless, we expect the short-range correlation effects will only modify quantitatively the behavior of the unstable solutions revealed in this work. Interesting modifications can also arise by introducing extrinsic disorder due to impurities and defects, which in some cases can significantly reduce the size of the entire coexistence region [41,42]. How these perturbations will affect the stability and the relevance of the domain wall matter we discussed here is a fascinating open problem which remains a challenge for future experiments as well as theory.

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