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### Large Magnetoresistance and Quantum Oscillations Observed in Superconducting $\beta$ -IrSn<sub>4</sub>

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#### Abstract

Diverse quantum phenomena have been observed in TSn<sub>4</sub> transition metal (T) stannides, including superconductivity, nontrivial topology, and large magnetoresistance at low temperatures. Here, we report the experimental and theoretical investigation of tetragonal  $\beta$ -IrSn<sub>4</sub> (space group  $I4_1/acd$ ) with the lattice parameters  $a = 6.362(3)$  Å and  $c = 22.723(0)$  Å. The temperature dependence of the electrical resistivity indicates that  $\beta$ -IrSn<sub>4</sub> is a good metal with Fermi-liquid behavior above the superconducting transition at  $T_c \sim 0.7$  K. Magnetic susceptibility measurements indicate it is non-magnetic. However, positive transverse magnetoresistance (MR) with linear field dependence is observed. At  $T = 2$  K and  $\mu_0H = 14$  T, the MR reaches 700% without sign of saturation. Shubnikov-de Haas (SdH) oscillations are observed from proximity detector oscillator (PDO) measurements up to 60 T. We experimentally extract several frequencies, and through comparison to first-principles calculations, identify corresponding electronic bands. For  $H \parallel c$ , two strong oscillations,  $F_1 \approx 109$  and  $F_2 \approx 302$  T, allow us to determine effective masses  $0.266m_0$  and  $0.300m_0$  ( $m_0$  is the free-electron mass), respectively. The topology of these bands is discussed.

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Electronic quantum materials represent a captivating field of exploration in condensed matter physics due to the variety of complex electronic behavior they exhibit and their potential to enable novel electronic devices [1-7]. The additional attraction of nontrivial topological properties, which have a wide range of potential impacts on physics, chemistry, and material science, has selected a subset of correlated-electron systems for more intensive study [1, 5-11]. Recent work from several transition metal stannides with the form  $TSn_4$  ( $T = Rh, Pd, Pt$ , etc.) strongly suggests the presence of unusual band structures with nontrivial topology that can trigger an abundance of phenomena, including large magnetoresistance (MR), quantized Hall effect, superconductivity, and strong quantum oscillations [12-20].

Owing to the polymorphic nature of high-tin content compounds, a number of the  $TSn_4$  compounds form polymorphs with different crystal structures [21-26]. For example,  $IrSn_4$  forms a trigonal structure ( $\alpha$ - $IrSn_4$ ) with either the  $P3_121$  (#152) or  $P3_221$  (#154) space group, a tetragonal structure ( $\beta$ - $IrSn_4$ ), and an orthorhombic structure ( $\gamma$ - $IrSn_4$ ). According to first-principles calculations,  $\alpha$ - $IrSn_4$  represents the ground state, requiring less energy than the other structures [22, 26]. Extremely large MR is observed in  $\alpha$ - $IrSn_4$ , which shows scaling behavior up to  $T = 50$  K that deviates from the standard Kohler's rule [17]. Superconductivity is not observed in resistivity measurements down to  $T = 0.1$  K in  $\alpha$ - $IrSn_4$ , despite its low residual resistivity ( $\rho_0 < 0.1 \mu\Omega \cdot cm$ ) [17, 26]. Structurally,  $\beta$ - $IrSn_4$  is more layered, with a lattice constant ratio  $c/a$  that is three times higher than those of  $\alpha$ - $IrSn_4$  and  $\gamma$ - $IrSn_4$  [20, 22, 26-28]. According to the *ab initio* calculations [29], there is a Van Hove singularity in the electronic structure of  $\beta$ - $IrSn_4$ , which is likely responsible for the superconductivity observed in this tetragonal polymorph [18]. This singularity is absent in other forms of  $IrSn_4$  [26, 29]. Therefore, a fundamental understanding of

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3 the electronic properties exhibited by each specific crystal structure of such polymorphic  
4 compounds is essential for uncovering rich quantum phenomena.  
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7 Among three polymorphs,  $\beta$ -IrSn<sub>4</sub> is least investigated. While its band structure is reported  
8 in Ref. [29], detailed information such as the quantum oscillation frequency, effective mass, and  
9 carrier type for each band is not available. On the other hand, MR for  $\beta$ -IrSn<sub>4</sub> is only measured up  
10 to 9 Tesla in Ref. [20], which is yet to be confirmed. In this article, we report a combination of  
11 experimental and theoretical investigation of the structural, magnetic, and electronic properties of  
12  $\beta$ -IrSn<sub>4</sub> single crystals. A large magnetoresistance (MR  $\sim$  700%) is observed at  $T = 2$  K and  $\mu_0H =$   
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14 14 T. Hall effect measurements reveal a decrease in the carrier concentration ( $n$ ) at low  
15 temperatures. Shubnikov-de Haas (SdH) oscillations are measured at various temperatures, angles,  
16 and field via the proximity detector oscillator (PDO) technique up to 60 T. From fast Fourier  
17 transformation (FFT) analysis of the SdH oscillations, two bands are identified, which are  
18 consistent with first-principles calculations. Information about the Berry phase and effective mass  
19 associated with each band is obtained as well.  
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22 Our IrSn<sub>4</sub> single crystals were grown using the self-flux (Sn) method. Iridium powder (*Alfa*  
23 *Aesar*, 99.9%) and tin granules (*BTC*, 99.9%) were combined in a molar ratio of 1 : 10 in an  
24 alumina crucible and sealed in an evacuated (pressure  $< 50$  mTorr) quartz ampoule. The mixture  
25 was heated to 1050°C at a rate of 50°C/h, held for 7 days, and cooled to 900°C at a rate of  $-4$  °C/h  
26 before being quenched in water. Excess Sn flux was removed by etching with a diluted  
27 hydrochloric acid (HCl) solution. The resulting crystals were flat and plate-like with a typical size  
28 of 0.8 mm ( $l$ )  $\times$  0.5 mm ( $w$ )  $\times$  0.07 mm ( $t$ ) as shown in Figure 1(a).  
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31 The crystal structure was determined through single crystal x-ray diffraction (XRD) using  
32 a PANalytical Empyrean x-ray diffractometer (Cu  $K\alpha$  radiation,  $\lambda_{K\alpha} = 1.5418$  Å). Electronic  
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3 structure calculations were performed using VASP (Vienna *ab-initio* Simulation Package) based  
4 on pseudo-potentials and a plane wave basis set [30]. The exchange-correlation energy functional  
5 was described using a PBE (GGA) scheme, taking the spin-orbit interaction (SOI) into account. A  
6 self-consistent calculation was performed using a gamma-centered  $16 \times 16 \times 4$   $k$ -point mesh with  
7 the plane-wave cutoff energy set to 300 eV. The Fermi surface was found using a  $k$ -point mesh of  
8  $61 \times 61 \times 61$  and visualized with the XCRYSDEN software [31].  
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11 Magnetization measurements were carried out in a Magnetic Property Measurement  
12 System (MPMS— 7 T, *Quantum Design*). The electrical resistivity, magnetoresistance, and Hall  
13 effect were recorded using a Physical Property Measurement System (PPMS— 14 T, *Quantum*  
14 *Design*). The contactless conductivity data was measured at various temperatures and magnetic  
15 field applied along different crystal axes using the PDO technique under pulsed magnetic fields of  
16 up to 60 T at the National High Magnetic Field Laboratory (NHMFL) [32]. A single crystal of  $\beta$ -  
17 IrSn<sub>4</sub> was placed on top of an 8-turn pancake coil made of 46-gauge copper wire. The coil is part  
18 of an LCR circuit driven by the PDO that has a resonant frequency in the range of 22-30 MHz  
19 [33]. Changes in the sample skin depth affect the inductance of the coil, producing a frequency  
20 shift  $\Delta f$ . If the sample is a metal,  $\Delta f \propto -\Delta \rho$ , where  $\Delta \rho$  is the corresponding change in the sample  
21 resistivity [33]. If the sample is an insulator,  $\Delta f$  is proportional to the magnetic susceptibility  
22 change [33]. As the PDO coil's field is localized and near surface, it is extremely sensitive to small  
23 changes. Compared resistivity and magnetic susceptibility measurements, PDO provides  
24 amplification via probing nonlinear contribution. The coil was mounted on a cryogenic goniometer  
25 that permits precise *in-situ* rotation at temperatures down to 0.5 K [34].  
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28 According to the single crystal XRD data, depicted in Figure 1(b), our IrSn<sub>4</sub> single crystals  
29 form in the MoSn<sub>4</sub>-type tetragonal structure, belonging to the space group *I4<sub>1</sub>/acd*. The lattice  
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parameters determined are  $a = 6.362(3)$  Å and  $c = 22.723(0)$  Å, resulting in  $c/a \sim 3.57$ . These values are consistent with previously reported results for the tetragonal  $\beta$ -IrSn<sub>4</sub> phase [18, 20] and differ from the lattice constants for the trigonal and orthorhombic phases [17, 20, 22, 26, 28, 35]. The structure of  $\beta$ -IrSn<sub>4</sub> can be described as four stacked layers of IrSn<sub>8</sub> antiprisms along the  $c$  direction as illustrated in Figure 1(c). This arrangement makes Ir-Sn-Sn-Ir-Sn-Sn-Ir... the favorable path for charge carriers to take in the  $c$  direction, suggesting that hybridization between  $p$ - $p$  (Sn-Sn) and  $p$ - $d$  (Sn-Ir) orbitals significantly affects the electrical transport properties [18, 20].

Figure 2(a) shows the temperature dependence of the zero-field in-plane resistivity ( $\rho_{xx}$ ) of  $\beta$ -IrSn<sub>4</sub> between temperatures  $T = 2$  K and 400 K. At room temperature ( $T \approx 300$  K),  $\rho_{xx} \approx 0.79$  mΩ·cm. This value is roughly one order of magnitude higher than that reported in Ref. [20]. However, we find that the residual resistivity ratio (RRR) is  $\rho_{xx}(300\text{ K})/\rho_{xx}(2\text{ K}) \approx 263$ , which is higher than that given in Ref. [20]. The larger RRR strongly suggests that our  $\beta$ -IrSn<sub>4</sub> crystals are of high quality and that the exploration of intrinsic low-temperature physical properties may prove fruitful [17-18, 26]. We can quantitatively fit the resistivity data using the Bloch-Grüneisen formula (Eq. (1)) for electron-phonon scattering:

$$\rho_{xx}(T) = \rho_0 + A \left( \frac{T}{\theta_D} \right)^3 \int_0^{\theta_D/T} \frac{x^3}{(e^x - 1)(1 - e^{-x})^2} dx, \quad (1)$$

where  $\rho_0$  is the residual resistivity,  $A$  is a constant describing electron-phonon coupling strength, and  $\theta_D$  is the Debye temperature. From this fit, represented by the red line in the main panel of Fig. 2(a), we obtain  $\rho_0 = (0.015 \pm 0.001)$  mΩ·cm,  $A = (2.1 \pm 0.2)$  mΩ·cm, and  $\theta_D = (201 \pm 5)$  K. Note that Eq. (1) fits our experimental data well over a wide temperature range (60 – 350 K). This fit implies that inter-band scattering is dominant in this system [36]. While the estimated Debye temperature is smaller than the previously reported values,  $\theta_D = 216$  K [18] and 256 K [20], we note that the  $A$  value is approximately 20 times larger than that obtained in Ref. [18], suggesting

there is significantly stronger electron-phonon coupling in our sample. In the inset of Fig. 2(a), the low-temperature  $\rho_{xx}(T)$  is plotted as  $\rho_{xx}(T)$  versus  $T^2$ , showing linear behavior persisting up to  $T \approx 70$  K. From fitting (orange line) the low-temperature data using  $\rho_{xx} = \rho_0^{LT} + A^{LT}T^2$ , we find  $\rho_0^{LT} = (2.1 \pm 0.3) \mu\Omega\cdot\text{cm}$  and  $A^{LT} = (2.59 \pm 0.01) \times 10^{-2} \mu\Omega\cdot\text{cm}\cdot\text{K}^{-2}$ .  $A^{LT}$  is significantly higher than typical values for transition metals ( $\sim 10^{-5} \mu\Omega\cdot\text{cm}\cdot\text{K}^{-2}$ ), suggesting relatively strong electron-electron interactions in the Fermi liquid state of  $\beta\text{-IrSn}_4$  [37]. This behavior may explain the noticeable differences between our low- $T$  data and those in Ref. [18], both in  $\rho_0^{LT}$  and the range over which the  $T^2$  behavior persists.

Following the precedents of de Haas-van Alphen (dHvA) oscillations in  $\text{PtSn}_4$  and superconductivity in  $\text{AuSn}_4$  and  $\beta\text{-IrSn}_4$  [14, 18-20], we examine the magnetic properties of our  $\beta\text{-IrSn}_4$  at low field ( $\mu_0H \leq 14$  T). The temperature dependence of the magnetic susceptibility  $\chi$ , shown in Figure 2(b), is measured between 2 K and 400 K with an applied field of  $\mu_0H = 1$  T along the  $c$ -axis in the zero-field-cooling (ZFC) mode. In the entire temperature region,  $\chi < 0$ , i.e. diamagnetic. To understand the nature of the magnetic response of  $\beta\text{-IrSn}_4$ , we fit the data using the Curie-Weiss (CW) formula:

$$\chi = \chi_0 + \frac{C}{T - \theta_{CW}}, \quad (2)$$

where  $\chi_0$  represents the temperature-independent contribution to the susceptibility,  $\theta_{CW}$  is the Curie-Weiss temperature, and  $C = N_A \mu_{eff}^2 / 3 k_B$  is the Curie-Weiss constant ( $N_A$  is the Avogadro constant,  $k_B$  is the Boltzmann constant, and  $\mu_{eff}$  is the effective magnetic moment). We obtain the following parameters from fitting:  $\chi_0 = (-7.770 \pm 0.004) \times 10^{-3} \text{ cm}^3/\text{mol}$ ,  $C = (0.0300 \pm 0.0002) \text{ cm}^3\cdot\text{K/mol}$ , and  $\theta_{CW} \sim 0$  K. From  $C$ , we find the effective magnetic moment  $\mu_{eff} = 0.15 \mu_B/\text{f.u.}$ . The zero  $\theta_{CW}$  and small  $\mu_{eff}$  indicate that there are negligible magnetic interactions in  $\beta\text{-IrSn}_4$ . By measuring the magnetic field dependence of the magnetization at a fixed temperature, linear

behavior is observed (not shown), indicating that the diamagnetic behavior results from the core contribution, i.e., a negative  $\chi_0$ .

Previous investigations of  $\beta$ -IrSn<sub>4</sub> reveal a superconducting transition at  $T_c \approx 0.9$  K – 1.05 K [18, 20]. From PDO measurements, we observe the resonant frequency ( $f$ ) increases below a critical field at  $T = 0.66$  K. Figure 2(c) shows the change in resonant frequency  $\Delta f$  with applied field at  $\theta = 4^\circ$  and  $91^\circ$  from the  $c$ -axis at  $T = 0.66$  K. Since  $\Delta f \propto -\Delta\rho$ , the sharp increase in  $\Delta f$  implies that  $\beta$ -IrSn<sub>4</sub> enters the superconducting state with an upper critical field of  $H_{c2}(4^\circ) \approx 0.17$  T and  $H_{c2}(91^\circ) \approx 0.3$  T at  $T = 0.66$  K. This value is much higher than that reported in Ref. [18, 20] at the same temperature, suggesting that the zero-field superconducting transition temperature is higher than 1.05 K [20]. The higher  $H_{c2}$ , and possibly higher  $T_c$ , is likely due to higher sample quality as reflected in the larger RRR.

In Ref. [20], the linear magnetoresistance (MR) was observed for the sample with a slightly lower RRR for  $H \parallel c$  at 2 K, which is attributed to open orbits. Figure 3(a) shows the field dependence of the MR up to 14 T at various temperatures. Two distinct features are immediately discernable: (1) at the measured temperatures ( $2 \text{ K} \leq T \leq 300 \text{ K}$ ), the MR varies almost linearly with  $H$  without sign of saturation and (2) MR increases with decreasing T reaching  $\sim 700\%$  at  $T = 2$  K and 14 T. In previous investigations,  $\text{MR}(9 \text{ T}) \sim 400\%$  at  $T = 2$  K was reported for  $\alpha$ -IrSn<sub>4</sub> (trigonal) [26] and  $\sim 820\%$  for  $\beta$ -IrSn<sub>4</sub> [20]. As discussed in Ref. [20], there linear MR is unlikely due to impurity effect, given that the high RRR for  $\beta$ -IrSn<sub>4</sub>. In the inset of Fig. 3(a), we plot MR vs.  $H/\rho_{xx}$  for each measured temperature with all collapsing into a single curve. This implies that electron scattering is governed by a single relaxation time, even though the MR is not proportional to  $H^2$  according to Kohler's scaling rule [38]. The deviation from the standard  $H$ -dependence of the MR may be related to the degree of the electron and hole compensation in semimetallic systems

[17, 37, 39]. Indeed, in isostructural  $\beta$ -RhSn<sub>4</sub> and PdSn<sub>4</sub>, the linear and unsaturated MR( $H$ ) is attributed to their semimetallic nature [12, 15].

To better understand the magnetotransport properties of  $\beta$ -IrSn<sub>4</sub>, the Hall resistivity  $\rho_{xy}$  is measured by applying  $H \parallel c$ . Figure 3(b) shows the field dependence of  $\rho_{xy}$  between 2 K and 300 K. Similar to that seen in  $\beta$ -RhSn<sub>4</sub> [12],  $\rho_{xy}$  is positive for  $\beta$ -IrSn<sub>4</sub>, suggesting the system is hole dominated. While the Hall resistivity varies linearly with  $\mu_0 H$  up to 14 T at  $T \geq 100$  K,  $\rho_{xy}(H)$  deviates from linearity at lower temperatures, which is consistent with observations in Refs. [18, 20]. To estimate the carrier concentration, we extract the Hall coefficient  $R_H$  by fitting  $\rho_{xy}(H)$  in the linear regime, i.e.,  $\mu_0 H \leq 1$  T. The value of  $R_H$  for each temperature is depicted in Figure 3(c), which exhibits a non-monotonic temperature dependence with a minimum occurring at  $T \sim 50$  K. Similar behavior is observed in PdSn<sub>4</sub> and PtSn<sub>4</sub> and is attributed to contributions from mixed holes and electrons [15, 16]. From  $R_H$ , we estimate the carrier concentration as shown Figure 3(d) with  $n \sim 2.7 \times 10^{21} \text{ cm}^{-3}$  at room temperature and  $\sim 2.5 \times 10^{21} \text{ cm}^{-3}$  at 2 K. This minor change in  $n$  suggests that the electronic structure is not severely modified by temperature.

From our observations of the behavior in the magnetoresistance and Hall resistivity, we seek further information about the electronic structure to answer our questions: (1) does the Fermi surface consist of both electron and hole bands? and (2) are there open orbits along the  $c$  direction as proposed in Ref. [20]? While quantum oscillations are not obvious from low field ( $\mu_0 H \leq 14$  T) measurements of  $\chi$  and MR, they are seen in PDO data measured under higher fields. Figure 4(a) shows the magnetic field dependence of the PDO frequency ( $f$ ) at  $T = 0.66$  K for the angle  $\theta(H \wedge c) = 4^\circ$ . After the initial sharp drop due to the superconducting transition,  $f$  decreases slowly with increasing field at all measured temperatures. We subtract a smooth background ( $f_{bg}$ ) after fitting the data to a 3<sup>rd</sup> order polynomial function. Figure 4(b) depicts  $\Delta f = f - f_{bg}$  in the high field

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3 regime where the oscillations are prominent. Here, oscillations with a periodicity proportional to  
4  $H^{-1}$  are discerned. Through fast Fourier transform (FFT) analysis, two oscillation frequencies are  
5 identified,  $F_1 = 109$  T and  $F_2 = 302$  T (Figure 4(c)). As PDO measures change in the skin depth of  
6 the coil, the oscillations in  $\Delta f$  reflect changes in the electrical conductivity, i.e., they are  
7 Shubnikov-de Haas (SdH) oscillations [33]. Thus, the two detected frequencies correspond to  
8 electron motion in two Fermi surface pockets [40]. We can construct a Landau-level (LL) fan  
9 diagram to characterize each pocket further as shown in Figure 4(d), where  $N$  is the LL index.  
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11 According to the Lifshitz-Onsager quantization criterion,  $N = \gamma + \frac{F_{fit}}{H}$ , with  $\gamma = \phi_B/2\pi + \delta$ . Here,  
12  $\phi_B$  is the Berry phase and  $\delta = 0, \frac{+1}{8}, \frac{-1}{8}$ , depending on carrier type and dimensionality of the Fermi  
13 surface [41]. By fitting the  $N(H^{-1})$  data using the Lifshitz-Onsager formula, we obtain  $\gamma$  and  $F_{fit}$   
14 for each oscillation, which are listed in Table I. As displayed in Fig. 4(c), the FFT amplitude for  
15 each oscillation decreases with increasing temperature. While the FFT spectrum is dominated by  
16 the lower frequency ( $F_1$ ), the higher frequency ( $F_2$ ) can also be well resolved up to  $T = 45$  K.  
17 Figures 4(e) and 4(f) display the temperature dependence of the FFT amplitude for  $F_1$  and  $F_2$ ,  
18 respectively. From a fit of the temperature dependence of the FFT amplitude to the thermal  
19 damping factor  $R_T = \frac{A'(\frac{m^*}{m_0})T}{\sinh(A'(\frac{m^*}{m_0})T)}$  ( $A'$  is a  $T$ -independent constant) of the Lifshitz-Kosevich  
20 formula [40], we obtain the effective masses  $m_{F1}^* = 0.266m_0$  and  $m_{F2}^* = 0.300m_0$ , where  $m_0$  is the  
21 free-electron mass.

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24 To understand the nature of the SdH oscillations, we perform electronic structure  
25 calculations. Using lattice relaxation calculations, we find that the system crystallizes in a  
26 tetragonal structure containing 40 atoms in the unit cell as shown in Figure 1(a). However, we  
27 obtain that  $a = b = 6.424$  Å and  $c = 23.108$  Å, slightly larger than those obtained from prior DFT  
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3 calculations [29] and our experimental work. The band structure is calculated along the high-  
4 symmetry directions of the tetragonal lattice using the path  $\Gamma - X - M - \Gamma - Z - R - A - Z|Z - R|M$   
5 –  $A$ , as shown in Figure 5. All bands not crossing the Fermi level are displayed in gray. There are  
6 eight bands (Bands I – VIII) contributing to the Fermi surface. Similar to prior work [29], there  
7 are several Dirac cones in the vicinity of the Fermi energy, which are denoted by circles in Figure  
8 5. The gaps in the encircled Dirac cones are  $\sim 10 - 20$  meV, also in agreement with Ref. [29]. The  
9 cones close to the Fermi energy distinguish  $\beta$ -IrSn<sub>4</sub> from many other topological semimetals with  
10 potential for future applications. The Fermi surface topology is presented in Figure 6 with both top  
11 ( $b_1, b_2$ ) and side ( $b_1, b_3$ ) views. Similar to a previously constructed Fermi surface [29], the bands  
12 exhibit mostly two-dimensional characteristic with open orbits along the  $c$ -direction. For each  
13 band, the expected oscillation frequency, effective mass, and carrier type are listed in Table I for  
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17 To figure out the origin of the experimentally observed oscillations at various angles, we  
18 plot the angle dependence of the frequencies obtained from FFT analysis, LL fan diagram fitting,  
19 and the theoretical frequency calculations in Figure 7. Through comparison, we find that Band II  
20 (Fig. 7(a)), IV (Fig. 7(b)), and VII (Fig. 7(d)) can have the oscillation  $F_1$ , and Band VII and VIII  
21 (Fig. 7(d)) can have  $F_2$  for  $H \parallel c$ . However, the angular dependence of the estimated frequency  
22 does not seem to close to that of  $F_{\text{th}}$  for Band II, which is thus not included in Table I. On the other  
23 hand, while not obvious in Fig. 4(c), the calculated frequencies for Band III match well with  
24 experimental data as shown in Fig. 7(b).  $F_{\text{th}}(H \parallel c) = 261$  T could be hidden under the broad peak  
25 marked as  $F_2$  in Fig. 4(c). Interestingly, all experimentally identified possible bands have electron  
26 character, as can be seen from Table I. Considering  $\beta$ -IrSn<sub>4</sub> is a hole-dominated system (Fig. 3 and  
27 Refs. [18, 20]), SdH oscillations from hole bands are likely too weak to be experimentally probed.  
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As listed in Table I, all calculated hole bands have high frequencies except Band V (which consists of a small pocket). In view of the FFT shown in Fig. 4(c), the strongest peak centered at  $F_1$  is broad. Low-frequency ( $< 200$  T) oscillations with much smaller amplitudes than the  $F_1$  oscillation are difficult to be identified from FFT. On the other hand, the experimentally identified  $F_{\text{ex}}(H \parallel c)$   $\sim 700$  T may result from a hole band (e.g. VI) but is too weak to be traced as the crystal orientation is rotated. Nevertheless, given the system involves multiple bands with both electron and hole pockets, the Hall coefficient should be expressed as  $R_H = \frac{1}{e} \frac{n_h \mu_h^2 - n_e \mu_e^2}{(\mu_h n_h + \mu_e n_e)^2}$ , where  $n_h$  is the hole carrier concentration,  $n_e$  denotes the electron concentration,  $\mu_h$  is the hole mobility, and  $\mu_e$  is the electron mobility. Even if  $n_h$  is lower than  $n_e$ , if  $\mu_h$  is much higher than  $\mu_e$ , the sign of  $R_H$  is determined by  $n_h \mu_h^2 - n_e \mu_e^2$ , leading to a positive sign. The nonlinear  $H$  dependence of  $\rho_{xy}$  below 50 K (Fig. 3(b)) reflects the change of  $n_h \mu_h^2 - n_e \mu_e^2$ . Despite experiment limitation, both calculated and experimental data presented in Fig. 7 will guide future work for  $\beta$ -IrSn<sub>4</sub>.

The  $\gamma$  values for some of the frequencies identified through LL fan diagrams are included in Table I. Based on theoretical calculations, we can further assign the  $\delta$  value for each case. The Berry phase  $\phi_B(H \parallel c)$  can thus be estimated as listed in Table I. It seems that Bands III, VI, and VII have a  $\phi_B(H \parallel c)$  close to  $\pi$ . In view of the band structure in Fig. 5, Band III is indeed associated with the three Dirac cones highlighted by three circles. If it dominates the electrical transport, the observed linear MR (Fig. 3(a)) can then be explained. While the large and linear MR could be related to open orbits [20, 42], we notice that (1) the linear MR is only seen for  $H \parallel c$  in  $\beta$ -IrSn<sub>4</sub> [20] and (2) the MR is the smallest for  $H \perp c$  [20] at which point the open orbits become most impactful (see Fig. 6). Therefore, the linear MR shown in Fig. 3(a) is unlikely due to open orbits. According to Ref. [43], the ratio MR/ $H$  scales linearly with the Berry curvature near the Fermi

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3 level. This is indeed the case for  $\beta$ -IrSn<sub>4</sub> (see Fig. 5). Further, the decrease of MR with increasing  
4 T is due to increased scattering or slowing down of carriers [43].  
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7 In summary, we have successfully grown IrSn<sub>4</sub> single crystals with the tetragonal structure,  
8 i.e.,  $\beta$ -IrSn<sub>4</sub>. Through both electrical resistivity and PDO measurements, we find that  $\beta$ -IrSn<sub>4</sub> is a  
9 metal with a superconducting ground state. While it is non-magnetic and clean, as reflected by a  
10 high RRR, a large transverse magnetoresistance of  $\sim 700\%$  is observed at  $T = 2$  K and  $\mu_0 H = 14$   
11 T. Although the MR at different temperatures and fields collapses into a single curve, its field  
12 dependence is nearly linear, not conforming to the standard Kohler's expression. By analyzing  
13 data collected from PDO measurements up to 60 T, Shubnikov-de Haas oscillations with various  
14 frequencies at different applied field directions are observed. Based on first-principles calculations,  
15 the Fermi surface of  $\beta$ -IrSn<sub>4</sub> consists of eight bands with band crossings along  $\Gamma - X - M - \Gamma$ . The  
16 experimentally observed frequencies  $F_1 = 109$  T and  $F_2 = 302$  T are most likely from Bands IV  
17 ( $F_1$ ), VI ( $F_1$ ), VII ( $F_1$ ), VII ( $F_2$ ), and VIII ( $F_2$ ), which all have electron character. By constructing  
18 Landau level fan diagrams, Berry phase for some bands can be extracted, pointing Bands III, VI,  
19 and VII with possible nontrivial topology. The nontrivial topology helps understand the linear MR  
20 ( $H \parallel c$ ) observed in a wide temperature range, similar to that reported in Ref. [43]. Further work  
21 is necessary to improve the experimental resolution for distinguishing oscillations and the accuracy  
22 of DFT calculations. According to Ref. [44], the van der Waals force can be important when  
23 calculating the band structures of layered materials, which may be relevant to  $\beta$ -IrSn<sub>4</sub>.  
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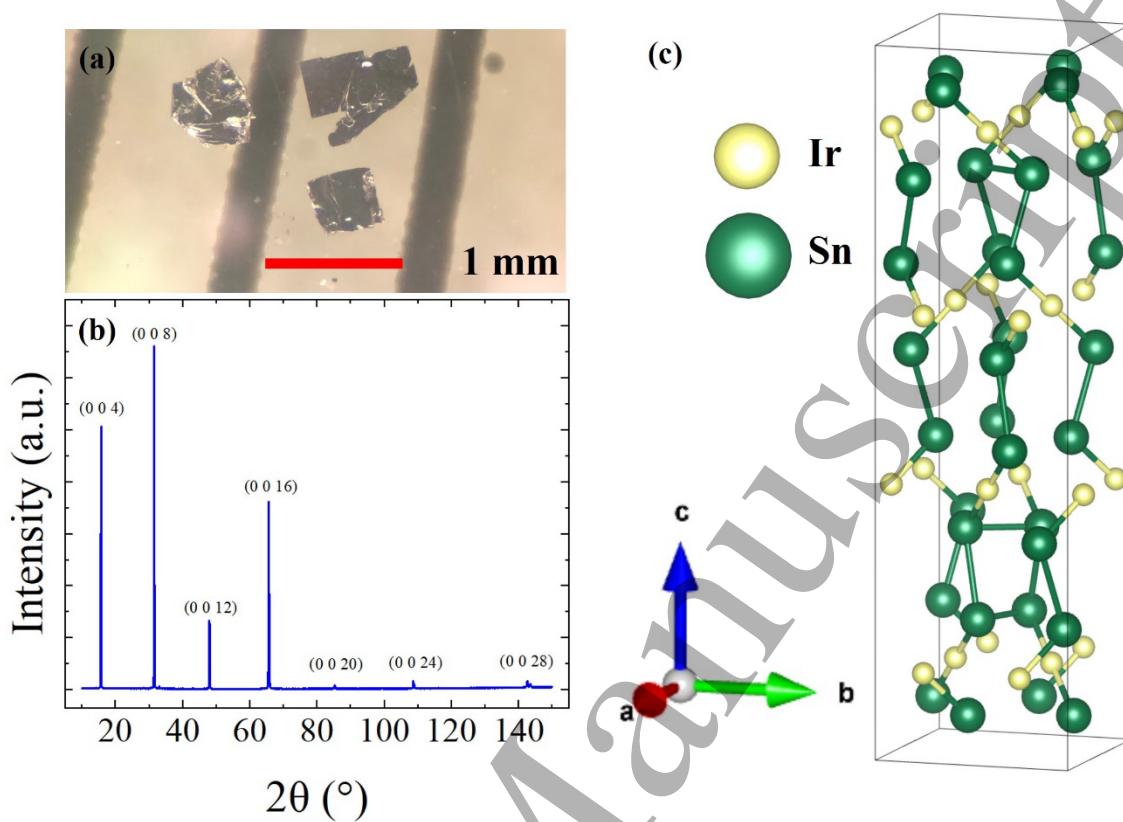
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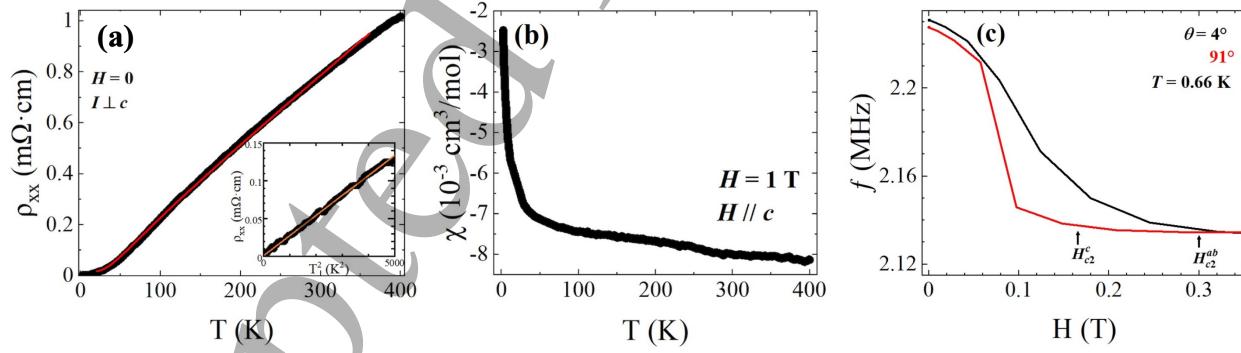
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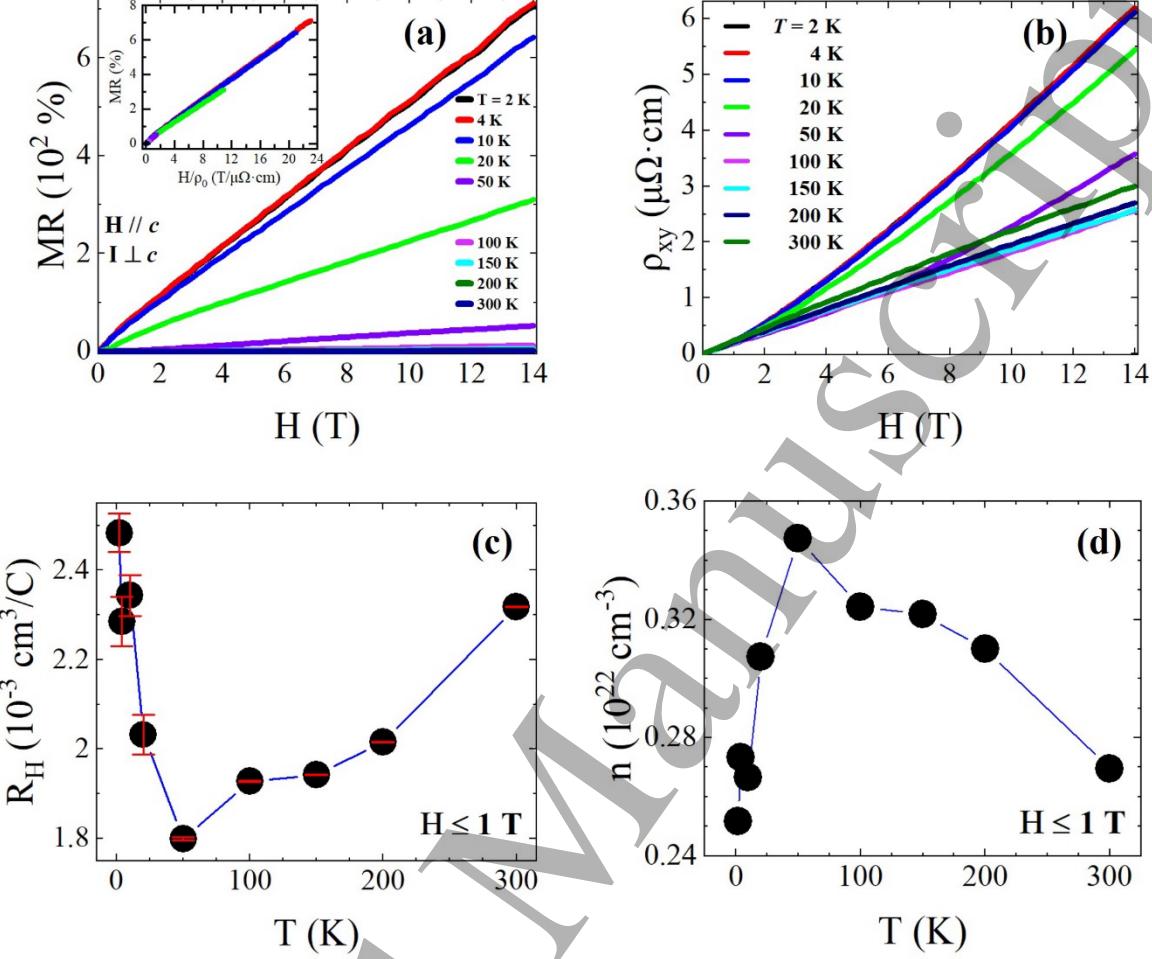
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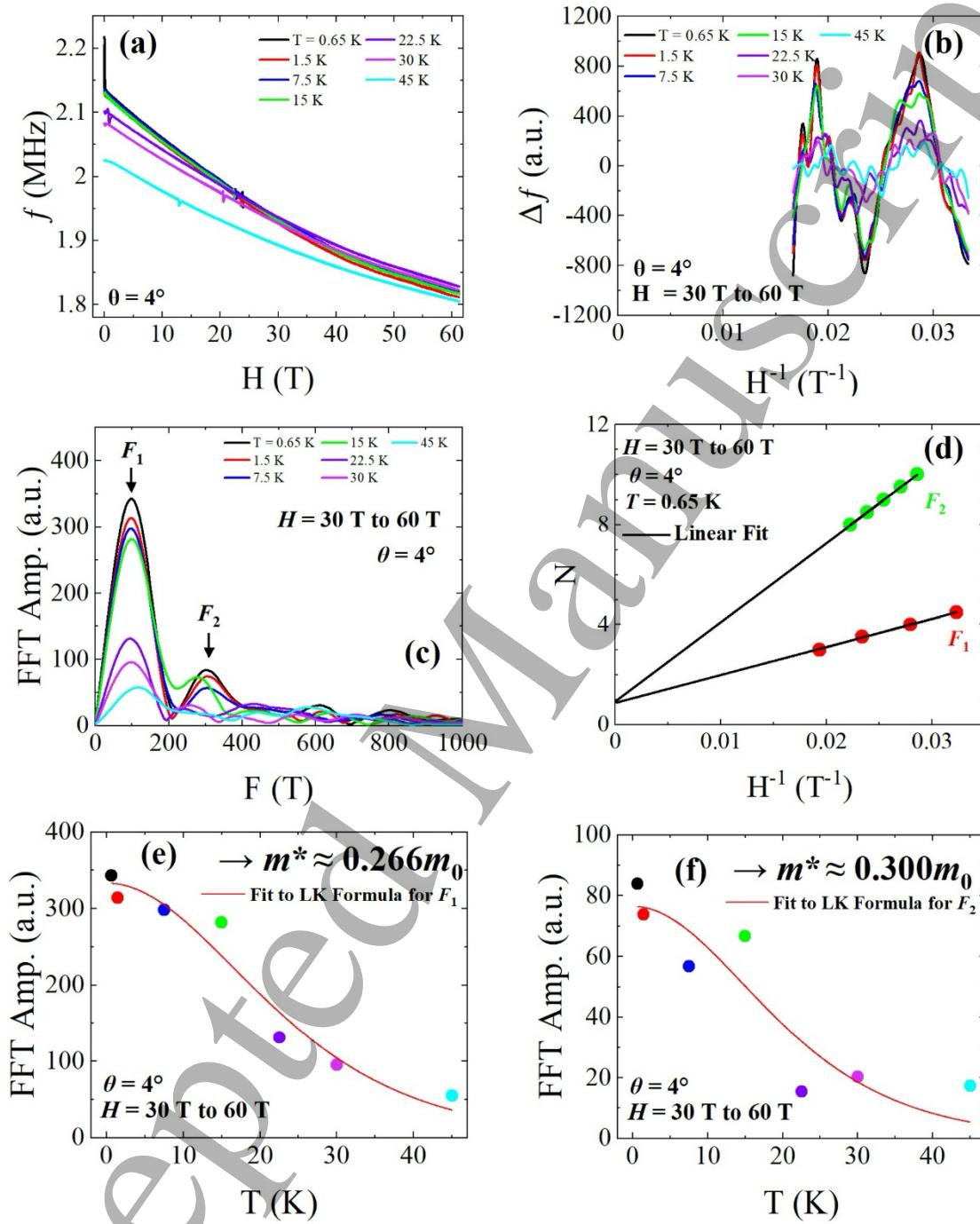
**Figure 1.** (a)  $\beta$ -IrSn<sub>4</sub> single crystals. (b) Room-temperature x-ray diffraction pattern on the surface of a single crystal. (c) Crystal structure of  $\beta$ -IrSn<sub>4</sub>.



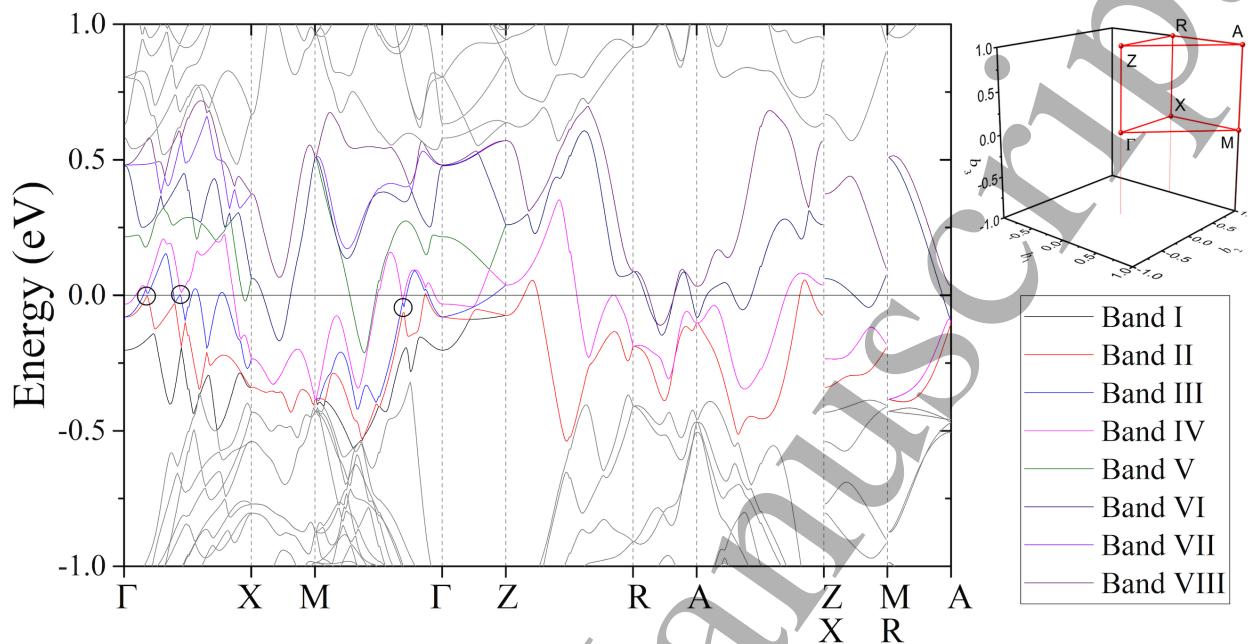
**Figure 2.** (a) Temperature dependence of the in-plane electrical resistivity ( $\rho_{xx}$ ). The red line in the main panel represents a fit to the Bloch-Grüneisen formula described in the text. Inset:  $\rho_{xx}$  versus  $T^2$  at low temperatures and the orange line represents a linear fit between 1.9 and 70 K as described in the text. (b) Temperature dependence of the magnetic susceptibility of  $\beta$ -IrSn<sub>4</sub> measured under an applied field of  $H = 1$  T in field-cooling (FC) mode with an orientation where  $H \parallel c$ . (c) Magnetic field dependence of the resonant frequency ( $f$ ) at  $T = 0.66$  K and indicated angles.



**Figure 3.** (a) Transverse MR vs.  $H$  at indicated temperatures. Inset: Kohler plot for  $\beta$ -IrSn<sub>4</sub> with the MR at all temperatures following into the same line. (b) Magnetic field dependence of the Hall resistivity ( $\rho_{xy}$ ) at indicated temperatures for  $H \parallel c$ . (c) Temperature dependence of the Hall coefficient ( $R_H$ ) obtained below 1 T. (d) Temperature dependence of the carrier concentration  $n$  described in the text.



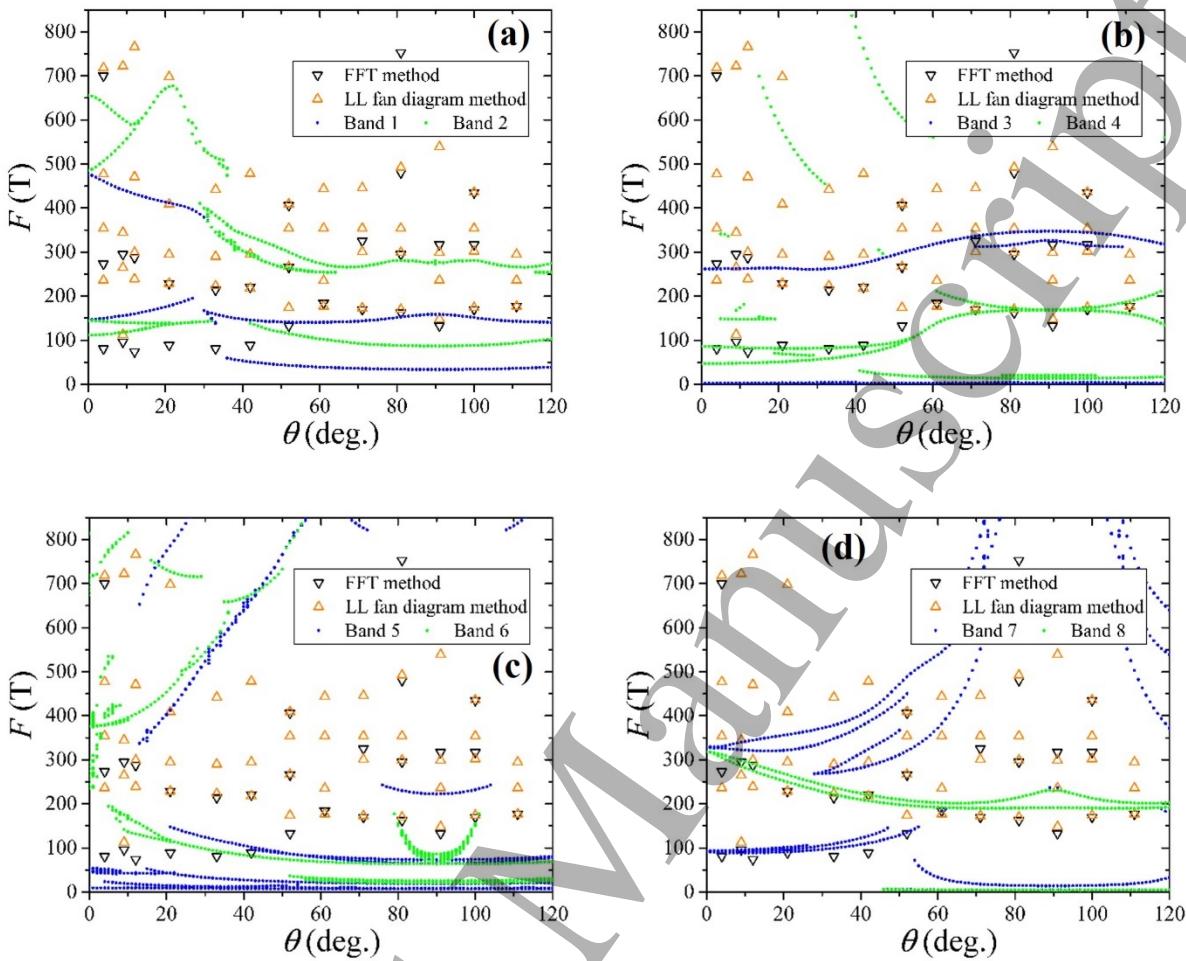
**Figure 4:** (a) Magnetic field dependence of  $f$  with  $H$  nearly parallel to the  $c$ -axis ( $\theta = 4^\circ$ ). (b) Shubnikov-de Haas (SdH) oscillations at various temperatures obtained through background subtraction. (c) FFT of data shown in (b). (d) Landau level (LL) fan diagram for two oscillations at  $T = 0.65$  K. (e) Temperature dependence of the FFT amplitude for  $F_1 \sim 109$  T at  $\theta = 4^\circ$ . (f) Temperature dependence of the FFT amplitude for  $F_2 \sim 302$  T at  $\theta = 4^\circ$ .



**Figure 5:** Band structure of  $\beta$ -IrSn<sub>4</sub> calculated accounting for spin-orbit interaction. Circles indicate the locations of Dirac cones. Special points of the Brillouin zone are defined. Bands not crossing the Fermi energy are shown in gray.

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**Figure 6:** Topology of the Fermi surface of  $\beta$ -IrSn<sub>4</sub> consisting of eight bands with both top ( $b_1$ ,  $b_2$ ) and side views ( $b_1$ ,  $b_3$ ).



**Figure 7:** Angular dependence of measured and calculated SdH frequencies. Calculated frequencies originating from different bands are shown in different plots for clarity: (a) Bands I and II; (b) Bands III and IV; (c) Bands V and VI; and (d) Bands VII and VIII.

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 3 Table I: Parameters obtained from the SdH oscillations for  $H \parallel c$  including the oscillation frequency ( $F$ ), intercept  
 4 ( $\gamma$ ), effective mass ( $m^*$ ), and corresponding Berry phase ( $\phi_B$ ). The calculated SdH frequency ( $F$ ), effective mass  
 5 ( $m^*$ ) and carrier type (electron( $e$ )/hole( $h$ )) character are also listed.  
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Band	Experiment ( $H \parallel c$ )					Theory ( $H \parallel c$ )		
	$F_{\text{FFT}}(\text{T})$	$\gamma$	$\delta$	$\phi_B (\pi)$	$m^*/m_0$	$F_{\text{th}}(\text{T})$	$m^*/m_0$	$e/h$
I						147	0.2781	$e$
						476	0.2637	$h$
II						111	0.2830	$e$
						144	0.2787	$e$
						504	0.2676	$h$
						679	0.5312	$h$
III	~250	0.62	-1/8	1.49		261	0.7849	$e$
						1221	0.3321	$h$
						1934	0.7337	$h$
IV	109	0.79	-1/8	1.83	0.266	47	0.2197	$e$
						86	0.2590	$e$
						1494	0.4237	$h$
						1853	0.3952	$e$
						1952	0.7293	$h$
V						49-56	0.3269-0.4176	$h$
						938	0.4039	$h$
VI						235	1.3746	$e$
						244	1.4101	$e$
						255	1.5467	$e$
						264	1.6454	$e$
						274	1.7855	$e$
						284	2.1411	$e$
						293	3.1404	$e$
						376	0.3125	$e$
						674	2.7291	$h$
						683	2.3082	$h$
						692	1.8769	$h$
VI	302	0.96	1/8	1.67		701	1.752	$h$
						708	1.5659	$h$
						718	1.4456	$h$
						814	0.8133	$h$
						814	0.8051	$h$
VII	109	0.79	1/8	1.33	0.266	91	0.1510	$e$
						94	0.1383	$e$
						328	0.2813	$e$
VIII	302	0.96	-1/8	0.23	0.300	330	0.2854	$e$
						318	0.2745	$e$